

# Higgs Boson Physics, Part I

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TASI 2004, Boulder

# Outline of Part I

- Understanding the **Electroweak Symmetry Breaking** as a first step towards a more fundamental theory of particle physics.
- **The Higgs mechanism** and the breaking of the Electroweak Symmetry in the Standard Model.
  - Toy model: breaking of an abelian gauge symmetry.
  - Quantum effects in spontaneously broken gauge theories.
  - The Standard Model: breaking of the  $SU(2)_L \times U(1)_Y$  symmetry.
  - Fermion masses through Yukawa-like couplings to the Higgs field.
- **First step: calculate the SM Higgs boson decay branching ratios.**

# Some References for Part I

- Spontaneous Symmetry Breaking of global and local symmetries:
  - ▷ An Introduction to Quantum Field Theory,  
M.E. Peskin and D.V. Schroeder
  - ▷ The Quantum Theory of Fields, V. II, S. Weinberg
- Theory and Phenomenology of the Higgs boson(s):
  - ▷ The Higgs Hunter Guide,  
J. Gunion, H.E. Haber, G. Kane, and S. Dawson
  - ▷ Introduction to the physics of Higgs bosons,  
S. Dawson, TASI Lectures 1994, hep-ph/9411325
  - ▷ Introduction to electroweak symmetry breaking,  
S. Dawson, hep-ph/9901280
  - ▷ Higgs Boson Theory and Phenomenology,  
M. Carena and H.E. Haber, hep-ph/0208209

# Breaking the Electroweak Symmetry: Why and How?

- The gauge symmetry of the Standard Model (SM) forbids gauge boson mass terms, but:

$$M_{W^\pm} = 80.426 \pm 0.034 \text{ GeV} \quad \text{and} \quad M_Z = 91.1875 \pm 0.0021 \text{ GeV}$$



## Electroweak Symmetry Breaking (EWSB)

- Broad spectrum of ideas proposed to explain the EWSB:
  - ▷ Weakly coupled dynamics embedded into some more fundamental theory at a scale  $\Lambda$  (probably  $\simeq$  TeV):
    - ⇒ Higgs Mechanism in the SM or its extensions (MSSM, etc.)
    - Little Higgs models
  - ▷ Strongly coupled dynamics at the TeV scale:
    - Technicolor in its multiple realizations.
  - ▷ Extra dimensions beyond the 3+1 space-time dimensions

## Different but related .....

- Explicit fermion mass terms also violate the gauge symmetry of the SM:
  - introduced through new gauge invariant interactions, as dictated by the mechanism of EWSB
  - intimately related to flavor mixing and the origin of CP-violation: new experimental evidence on this side will give further insight.

# The story begins in 1964 ...

with Englert and Brout; Higgs; Hagen, Guralnik and Kibble

VOLUME 13, NUMBER 9

PHYSICAL REVIEW LETTERS

31 AUGUST 1964

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## BROKEN SYMMETRY AND THE MASS OF GAUGE VECTOR MESONS\*

F. Englert and R. Brout

Faculté des Sciences, Université Libre de Bruxelles, Bruxelles, Belgium

(Received 26 June 1964)

VOLUME 13, NUMBER 16

PHYSICAL REVIEW LETTERS

19 OCTOBER 1964

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## BROKEN SYMMETRIES AND THE MASSES OF GAUGE BOSONS

Peter W. Higgs

Tait Institute of Mathematical Physics, University of Edinburgh, Edinburgh, Scotland

(Received 31 August 1964)

VOLUME 13, NUMBER 20

PHYSICAL REVIEW LETTERS

16 NOVEMBER 1964

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## GLOBAL CONSERVATION LAWS AND MASSLESS PARTICLES\*

G. S. Guralnik,<sup>†</sup> C. R. Hagen,<sup>‡</sup> and T. W. B. Kibble

Department of Physics, Imperial College, London, England

(Received 12 October 1964)

# Spontaneous Breaking of a Gauge Symmetry

**Abelian Higgs mechanism:** one vector field  $A^\mu(x)$  and one complex scalar field  $\phi(x)$ :

$$\mathcal{L} = \mathcal{L}_A + \mathcal{L}_\phi$$

where

$$\mathcal{L}_A = -\frac{1}{4}F^{\mu\nu}F_{\mu\nu} = -\frac{1}{4}(\partial^\mu A^\nu - \partial^\nu A^\mu)(\partial_\mu A_\nu - \partial_\nu A_\mu)$$

and  $(D^\mu = \partial^\mu + igA^\mu)$

$$\mathcal{L}_\phi = (D^\mu \phi)^* D_\mu \phi - V(\phi) = (D^\mu \phi)^* D_\mu \phi - \mu^2 \phi^* \phi - \lambda(\phi^* \phi)^2$$

$\mathcal{L}$  invariant under local phase transformation, or local  $U(1)$  symmetry:

$$\begin{aligned}\phi(x) &\rightarrow e^{i\alpha(x)} \phi(x) \\ A^\mu(x) &\rightarrow A^\mu(x) + \frac{1}{g} \partial^\mu \alpha(x)\end{aligned}$$

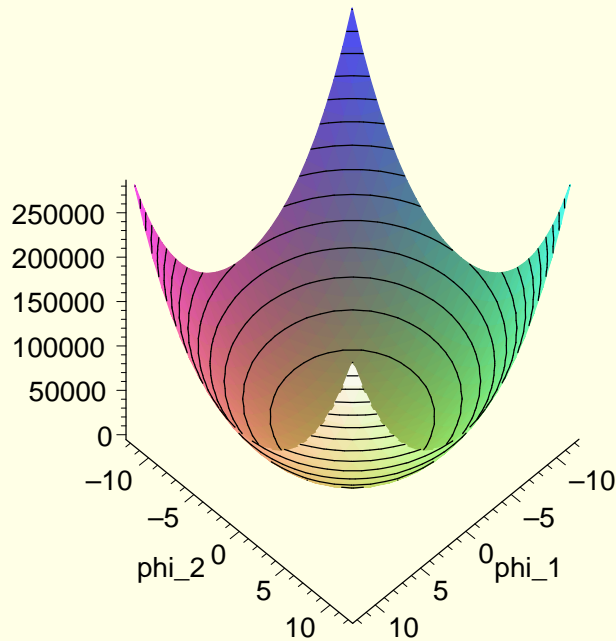
Mass term for  $A^\mu$  breaks the  $U(1)$  gauge invariance.

Can we build a gauge invariant massive theory? Yes.

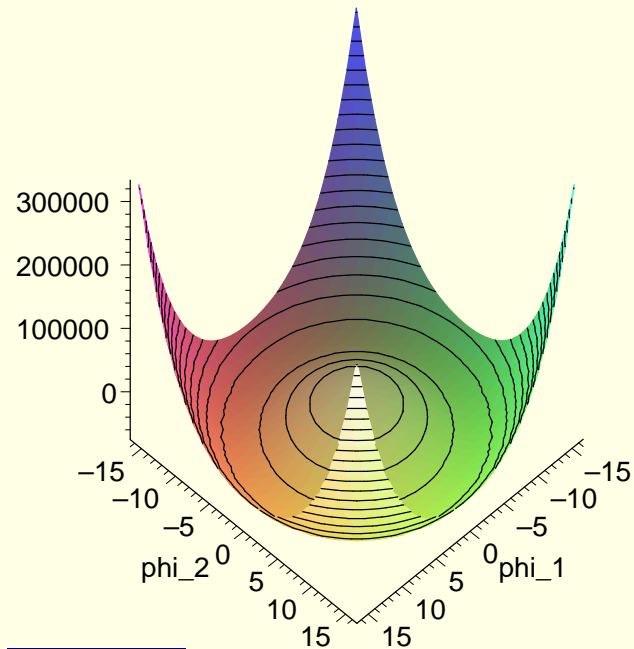
Consider the potential of the scalar field:

$$V(\phi) = \mu^2 \phi^* \phi + \lambda (\phi^* \phi)^2$$

where  $\lambda > 0$  (to be bounded from below), and observe that:



$\mu^2 > 0$  → unique minimum:  
 $\phi^* \phi = 0$



$\mu^2 < 0$  → degeneracy of minima:  
 $\phi^* \phi = \frac{-\mu^2}{2\lambda}$



- $\mu^2 > 0 \longrightarrow$  electrodynamics of a massless photon and a massive scalar field of mass  $\mu$  ( $g = -e$ ).
- $\mu^2 < 0 \longrightarrow$  when we choose a minimum, the original  $U(1)$  symmetry is spontaneously broken or hidden.

$$\phi_0 = \left( -\frac{\mu^2}{2\lambda} \right)^{1/2} = \frac{v}{\sqrt{2}} \longrightarrow \phi(x) = \phi_0 + \frac{1}{\sqrt{2}} (\phi_1(x) + i\phi_2(x))$$

$\Downarrow$

$$\mathcal{L} = \underbrace{-\frac{1}{4}F^{\mu\nu}F_{\mu\nu} + \frac{1}{2}g^2v^2A^\mu A_\mu}_{\text{massive vector field}} + \underbrace{\frac{1}{2}(\partial^\mu\phi_1)^2 + \mu^2\phi_1^2}_{\text{massive scalar field}} + \underbrace{\frac{1}{2}(\partial^\mu\phi_2)^2 + gvA_\mu\partial^\mu\phi_2 + \dots}_{\text{Goldstone boson}}$$

**Side remark:** The  $\phi_2$  field actually generates the correct transverse structure for the mass term of the (now massive)  $A^\mu$  field propagator:

$$\langle A^\mu(k)A^\nu(-k) \rangle = \frac{-i}{k^2 - m_A^2} \left( g^{\mu\nu} - \frac{k^\mu k^\nu}{k^2} \right) + \dots$$

More convenient parameterization (unitary gauge):

$$\phi(x) = \frac{e^{i\frac{\chi(x)}{v}}}{\sqrt{2}}(v + H(x)) \xrightarrow{U(1)} \frac{1}{\sqrt{2}}(v + H(x))$$

The  $\chi(x)$  degree of freedom (Goldstone boson) is rotated away using gauge invariance, while the original Lagrangian becomes:

$$\mathcal{L} = \mathcal{L}_A + \frac{g^2 v^2}{2} A^\mu A_\mu + \frac{1}{2} (\partial^\mu H \partial_\mu H + 2\mu^2 H^2) + \dots$$

which describes now the dynamics of a system made of:

- a massive vector field  $A^\mu$  with  $m_A^2 = g^2 v^2$ ;
- a real scalar field  $H$  of mass  $m_H^2 = -2\mu^2 = 2\lambda v^2$ : the Higgs field.



Total number of degrees of freedom is balanced

**Non-Abelian Higgs mechanism:** several vector fields  $A_\mu^a(x)$  and several (real) scalar field  $\phi_i(x)$ :

$$\mathcal{L} = \mathcal{L}_A + \mathcal{L}_\phi \quad , \quad \mathcal{L}_\phi = \frac{1}{2}(D^\mu \phi)^2 - V(\phi) \quad , \quad V(\phi) = \mu^2 \phi^2 + \frac{\lambda}{2} \phi^4$$

( $\mu^2 < 0$ ,  $\lambda > 0$ ) invariant under a non-Abelian symmetry group  $G$ :

$$\phi_i \longrightarrow (1 + i\alpha^a t^a)_{ij} \phi_j \xrightarrow{t^a = iT^a} (1 - \alpha^a T^a)_{ij} \phi_j$$

(s.t.  $D_\mu = \partial_\mu + gA_\mu^a T^a$ ). In analogy to the Abelian case:

$$\begin{aligned} \frac{1}{2}(D_\mu \phi)^2 &\longrightarrow \dots + \frac{1}{2}g^2 (T^a \phi)_i (T^b \phi)_i A_\mu^a A^{b\mu} + \dots \\ &\xrightarrow{\phi_{min} = \phi_0} \dots + \frac{1}{2} \underbrace{g^2 (T^a \phi_0)_i (T^b \phi_0)_i}_{m_{ab}^2} A_\mu^a A^{b\mu} + \dots = \end{aligned}$$

$$\boxed{T^a \phi_0 \neq 0} \longrightarrow \text{massive vector boson} + (\text{Goldstone boson})$$

$$\boxed{T^a \phi_0 = 0} \longrightarrow \text{massless vector boson} + \text{massive scalar field}$$

Classical  $\longrightarrow$  Quantum :

$$V(\phi) \longrightarrow V_{eff}(\varphi_{cl})$$

The stable vacuum configurations of the theory are now determined by the extrema of the Effective Potential:

$$V_{eff}(\varphi_{cl}) = -\frac{1}{VT} \Gamma_{eff}[\phi_{cl}] \quad , \quad \phi_{cl} = \text{constant} = \varphi_{cl}$$

where

$$\Gamma_{eff}[\phi_{cl}] = W[J] - \int d^4y J(y) \phi_{cl}(y) \quad , \quad \phi_{cl}(x) = \frac{\delta W[J]}{\delta J(x)} = \langle 0 | \phi(x) | 0 \rangle_J$$

$W[J] \longrightarrow$  generating functional of connected correlation functions

$\Gamma_{eff}[\phi_{cl}] \longrightarrow$  generating functional of 1PI connected correlation functions

$V_{eff}(\varphi_{cl})$  can be organized as a loop expansion (expansion in  $\hbar$ ), s.t.:

$$V_{eff}(\varphi_{cl}) = V(\varphi_{cl}) + \text{loop effects}$$

SSB  $\longrightarrow$  non trivial vacuum configurations

Gauge fixing : the  $R_\xi$  gauges. Consider the abelian case:

$$\mathcal{L} = -\frac{1}{4}F^{\mu\nu}F_{\mu\nu} + (D^\mu\phi)^*D_\mu\phi - V(\phi)$$

upon SSB:

$$\phi(x) = \frac{1}{\sqrt{2}}((v + \phi_1(x)) + i\phi_2(x))$$

$\Downarrow$

$$\mathcal{L} = -\frac{1}{4}F^{\mu\nu}F_{\mu\nu} + \frac{1}{2}(\partial^\mu\phi_1 + gA^\mu\phi_2)^2 + \frac{1}{2}(\partial^\mu\phi_2 - gA^\mu(v + \phi_1))^2 - V(\phi)$$

Quantizing using the gauge fixing condition:

$$G = \frac{1}{\sqrt{\xi}}(\partial_\mu A^\mu + \xi g v \phi_2)$$

in the generating functional

$$Z = C \int \mathcal{D}A \mathcal{D}\phi_1 \mathcal{D}\phi_2 \exp \left[ \int d^4x \left( \mathcal{L} - \frac{1}{2}G^2 \right) \right] \det \left( \frac{\delta G}{\delta \alpha} \right)$$

( $\alpha \longrightarrow$  gauge transformation parameter)

$$\begin{aligned}
\mathcal{L} - \frac{1}{2}G^2 &= -\frac{1}{2}A_\mu \left( -g^{\mu\nu} \partial^2 + \left(1 - \frac{1}{\xi}\right) \partial^\mu \partial^\nu - (gv)^2 g^{\mu\nu} \right) A_\nu \\
&\quad + \frac{1}{2}(\partial_\mu \phi_1)^2 - \frac{1}{2}m_{\phi_1}^2 \phi_1^2 + \frac{1}{2}(\partial_\mu \phi_2)^2 - \frac{\xi}{2}(gv)^2 \phi_2^2 + \dots \\
\mathcal{L}_{ghost} &= \bar{c} \left[ -\partial^2 - \xi(gv)^2 \left(1 + \frac{\phi_1}{v}\right) \right] c
\end{aligned}$$

such that:

$$\begin{aligned}
\langle A^\mu(k) A^\nu(-k) \rangle &= \frac{-i}{k^2 - m_A^2} \left( g^{\mu\nu} - \frac{k^\mu k^\nu}{k^2} \right) + \frac{-i\xi}{k^2 - \xi m_A^2} \left( \frac{k^\mu k^\nu}{k^2} \right) \\
\langle \phi_1(k) \phi_1(-k) \rangle &= \frac{-i}{k^2 - m_{\phi_1}^2} \\
\langle \phi_2(k) \phi_2(-k) \rangle &= \langle c(k) \bar{c}(-k) \rangle = \frac{-i}{k^2 - \xi m_A^2}
\end{aligned}$$

Goldstone boson $\phi_2$ , $\iff$ longitudinal gauge bosons
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The Higgs sector of the Standard Model :

$$SU(2)_L \times U(1)_Y \xrightarrow{SSB} U(1)_Q$$

Introduce one complex scalar doublet of  $SU(2)_L$  with  $Y=1/2$ :

$$\phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix} \longleftrightarrow \mathcal{L} = (D^\mu \phi)^\dagger D_\mu \phi - \mu^2 \phi^\dagger \phi - \lambda (\phi^\dagger \phi)^2$$

where  $D_\mu \phi = (\partial_\mu - igA_\mu^a \tau^a - ig'Y_\phi B_\mu)$ , ( $\tau^a = \sigma^a/2$ ,  $a=1, 2, 3$ ).

The SM symmetry is spontaneously broken when  $\langle \phi \rangle$  is chosen to be (e.g.):

$$\langle \phi \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v \end{pmatrix} \quad \text{with} \quad v = \left( \frac{-\mu^2}{\lambda} \right)^{1/2} \quad (\mu^2 < 0, \lambda > 0)$$

The gauge boson mass terms arise from:

$$\begin{aligned} (D^\mu \phi)^\dagger D_\mu \phi &\longrightarrow \dots + \frac{1}{8} (0 \ v) (gA_\mu^a \sigma^a + g' B_\mu) (gA^{b\mu} \sigma^b + g' B^\mu) \begin{pmatrix} 0 \\ v \end{pmatrix} + \dots \\ &\longrightarrow \dots + \frac{1}{2} \frac{v^2}{4} [g^2 (A_\mu^1)^2 + g^2 (A_\mu^2)^2 + (-gA_\mu^3 + g' B_\mu)^2] + \dots \end{aligned}$$

And correspond to the weak gauge bosons:

$$W_{\mu}^{\pm} = \frac{1}{\sqrt{2}}(A_{\mu}^1 \pm A_{\mu}^2) \longrightarrow \boxed{M_W = g \frac{v}{2}}$$

$$Z_{\mu}^0 = \frac{1}{\sqrt{g^2 + g'^2}}(gA_{\mu}^3 - g'B_{\mu}) \longrightarrow \boxed{M_Z = \sqrt{g^2 + g'^2} \frac{v}{2}}$$

while the linear combination orthogonal to  $Z_{\mu}^0$  remains massless and corresponds to the photon field:

$$A_{\mu} = \frac{1}{\sqrt{g^2 + g'^2}}(g'A_{\mu}^3 + gB_{\mu}) \longrightarrow \boxed{M_A = 0}$$

**Notice:** using the definition of the weak mixing angle,  $\theta_w$ :

$$\cos \theta_w = \frac{g}{\sqrt{g^2 + g'^2}}, \quad \sin \theta_w = \frac{g'}{\sqrt{g^2 + g'^2}}$$

the  $W$  and  $Z$  masses are related by:  $\boxed{M_W = M_Z \cos \theta_w}$



The scalar sector becomes more transparent in the unitary gauge:

$$\phi(x) = \frac{e^{\frac{i}{v}\vec{\chi}(x)\cdot\vec{\tau}}}{\sqrt{2}} \begin{pmatrix} 0 \\ v + H(x) \end{pmatrix} \xrightarrow{SU(2)} \phi(x) = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v + H(x) \end{pmatrix}$$

after which the Lagrangian becomes

$$\mathcal{L} = \mu^2 H^2 - \lambda v H^3 - \frac{1}{4} H^4 = -\frac{1}{2} M_H^2 H^2 - \sqrt{\frac{\lambda}{2}} M_H H^3 - \frac{1}{4} \lambda H^4$$

Three degrees of freedom, the  $\chi^a(x)$  Goldstone bosons, have been reabsorbed into the longitudinal components of the  $W_\mu^\pm$  and  $Z_\mu^0$  weak gauge bosons. One real scalar field remains:

the Higgs boson, H, with mass  $M_H^2 = -2\mu^2 = 2\lambda v^2$

and self-couplings:

$$\begin{array}{c} \text{H} \\ \diagdown \\ \text{---} \\ \diagup \\ \text{H} \end{array} \text{---} \text{H} = -3i \frac{M_H^2}{v}$$

$$\begin{array}{cc} \text{H} & \text{H} \\ \diagdown & \diagup \\ & \text{---} \\ \diagup & \diagdown \\ \text{H} & \text{H} \end{array} = -3i \frac{M_H^2}{v^2}$$

From  $(D^\mu \phi)^\dagger D_\mu \phi \longrightarrow$  Higgs-Gauge boson couplings:

$$= 2i \frac{M_V^2}{v} g^{\mu\nu}$$

$$= 2i \frac{M_V^2}{v^2} g^{\mu\nu}$$

**Notice:** The entire Higgs sector depends on only **two parameters**, e.g.

$M_H$  and  $v$

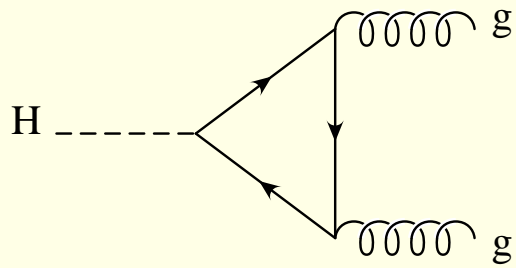
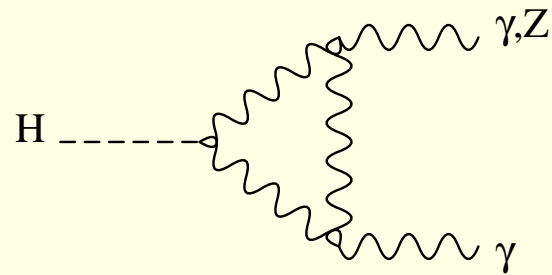
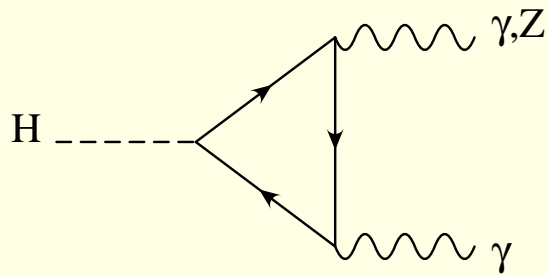
$v$  measured in  $\mu$ -decay:

$$v = (\sqrt{2}G_F)^{-1/2} = 246 \text{ GeV}$$

$\longrightarrow$

SM Higgs Physics depends on  $M_H$

Also: remember Higgs-gauge boson loop-induced couplings:



They will be discussed in the context of Higgs boson decays.

## Finally: Higgs boson couplings to quarks and leptons

The gauge symmetry of the SM also forbids fermion mass terms ( $m_{Q_i} Q_L^i u_R^i, \dots$ ), but all fermions are massive.



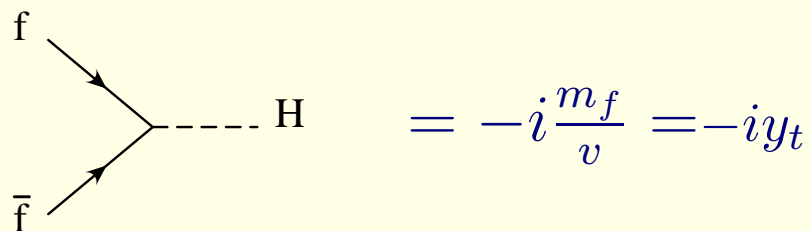
Fermion masses are generated via gauge invariant Yukawa couplings:

$$\mathcal{L}_{Yukawa} = -\Gamma_u^{ij} \bar{Q}_L^i \phi^c u_R^j - \Gamma_d^{ij} \bar{Q}_L^i \phi d_R^j - \Gamma_e^{ij} \bar{L}_L^i \phi l_R^j + h.c.$$

such that, upon spontaneous symmetry breaking:

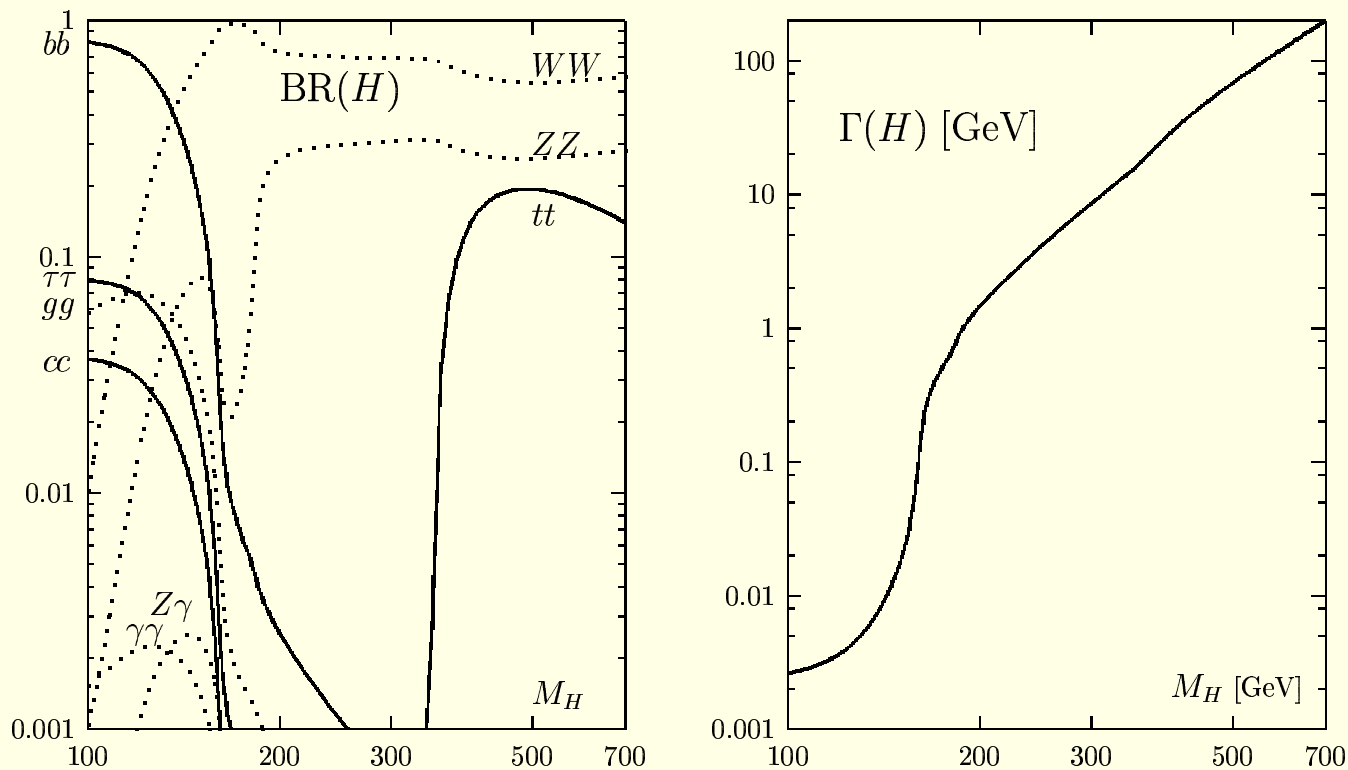
$$\phi(x) = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v + H(x) \end{pmatrix} \longrightarrow \boxed{m_f = \Gamma_f \frac{v}{\sqrt{2}}}$$

and


$$\begin{array}{c} f \\ \swarrow \\ \text{---} \\ \searrow \\ \bar{f} \end{array} \text{---} H = -i \frac{m_f}{v} = -i y_f$$

# SM Higgs boson decay branching ratios

We can now calculate branching ratios and total width of the SM Higgs boson:



Observe difference between light and heavy Higgs

These curves include: tree level + QCD and EW loop corrections.

## Tree level decays: $H \rightarrow f\bar{f}$ and $H \rightarrow VV$

At lowest order:

$$\Gamma(H \rightarrow f\bar{f}) = \frac{G_F M_H}{4\sqrt{2}\pi} N_{cf} m_f^2 \beta_f^3$$

$$\Gamma(H \rightarrow VV) = \frac{G_F M_H^3}{16\sqrt{2}\pi} \delta_V \left( 1 - \tau_V + \frac{3}{4}\tau_V^2 \right) \beta_V$$

$$(\beta_i = \sqrt{1 - \tau_i}, \tau_i = 4m_i^2/M_H^2, \delta_{W,Z} = 2, 1, (N_c)_{l,q} = 1, 3)$$

**Ex.1:** Higher order corrections to  $H \rightarrow q\bar{q}$

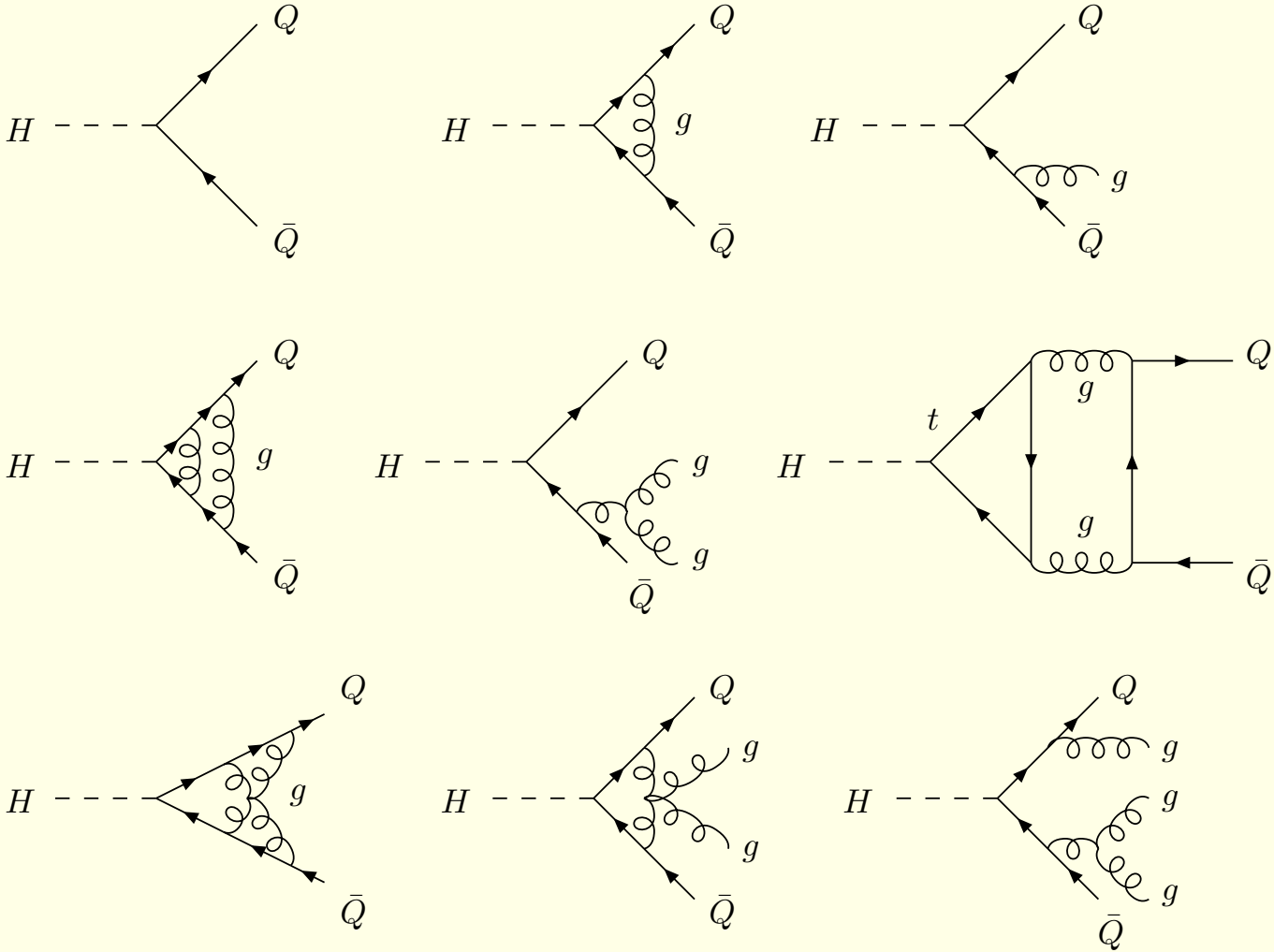
QCD corrections dominant:

$$\Gamma(H \rightarrow q\bar{q})_{\text{QCD}} = \frac{3G_F M_H}{4\sqrt{2}\pi} \bar{m}_q^2(M_H) \beta_q^3 [\Delta_{\text{QCD}} + \Delta_t]$$

$$\Delta_{\text{QCD}} = 1 + 5.67 \frac{\alpha_s(M_H)}{\pi} + (35.94 - 1.36N_F) \left( \frac{\alpha_s(M_H)}{\pi} \right)^2$$

$$\Delta_t = \left( \frac{\alpha_s(M_H)}{\pi} \right)^2 \left[ 1.57 - \frac{2}{3} \ln \frac{M_H^2}{m_t^2} + \frac{1}{9} \ln^2 \frac{\bar{m}_q^2(M_H)}{M_H^2} \right]$$

Consist of both virtual and real corrections:



- Large Logs absorbed into  $\overline{MS}$  quark mass

$$\text{Leading Order : } \bar{m}_Q(\mu) = \bar{m}_Q(m_Q) \left( \frac{\alpha_s(\mu)}{\alpha_s(m_Q)} \right)^{\frac{2b_0}{\gamma_0}}$$

$$\text{Higher order : } \bar{m}_Q(\mu) = \bar{m}_Q(m_Q) \frac{f(\alpha_s(\mu)/\pi)}{f(\alpha_s(m_Q)/\pi)}$$

where (from renormalization group equation)

$$f(x) = \left( \frac{25}{6} x \right)^{\frac{12}{25}} [1 + 1.014x + \dots] \quad \text{for } m_c < \mu < m_b$$

$$f(x) = \left( \frac{23}{6} x \right)^{\frac{12}{23}} [1 + 1.175x + \dots] \quad \text{for } m_b < \mu < m_t$$

$$f(x) = \left( \frac{7}{2} x \right)^{\frac{4}{7}} [1 + 1.398x + \dots] \quad \text{for } \mu > m_t$$

- Large corrections, when  $M_H \gg m_Q$

$$m_b(m_b) \simeq 4.2 \text{ GeV} \longrightarrow \bar{m}_b(M_h \simeq 100 \text{ GeV}) \simeq 3 \text{ GeV}$$

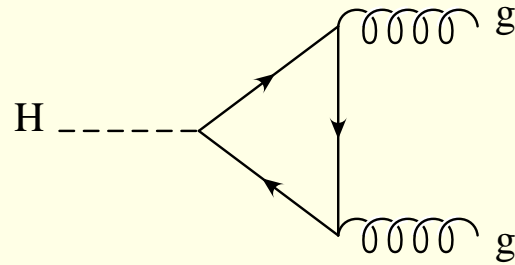
Branching ratio smaller by almost a factor 2.

- Main uncertainties:  $\alpha_s(M_Z)$ , pole masses:  $m_c(m_c)$ ,  $m_b(m_b)$ .



**Ex. 2:** Higher order corrections  $\Gamma(H \rightarrow gg)$

Start from tree level:



$$\Gamma(H \rightarrow gg) = \frac{G_F \alpha_s^2 M_H^3}{36 \sqrt{2} \pi^3} \left| \sum_q A_q^H(\tau_q) \right|$$

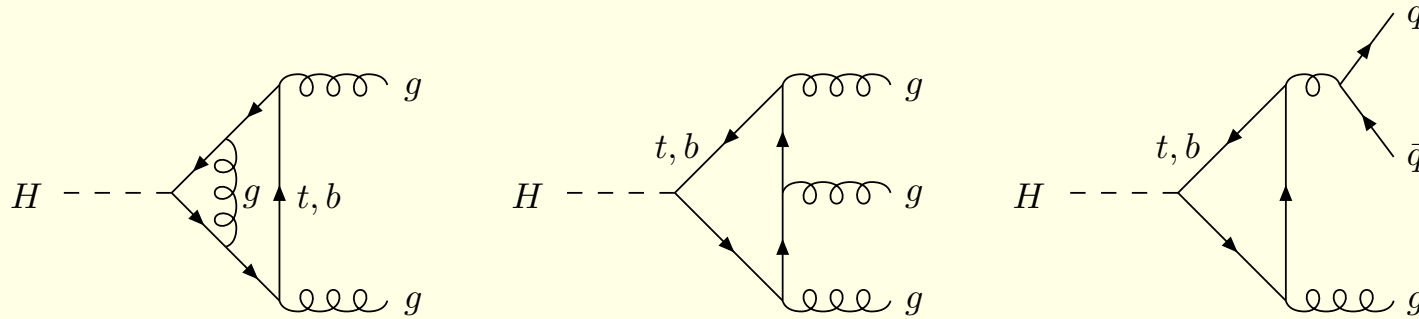
where  $\tau_q = 4m_q^2/M_H^2$  and

$$A_q^H(\tau) = \frac{3}{2} \tau [1 + (1 - \tau) f(\tau)]$$

$$f(\tau) = \begin{cases} \arcsin^2 \frac{1}{\sqrt{\tau}} & \tau \geq 1 \\ -\frac{1}{4} \left[ \ln \frac{1 + \sqrt{1 - \tau}}{1 - \sqrt{1 - \tau}} - i\pi \right]^2 & \tau < 1 \end{cases}$$

Main contribution from top quark  $\rightarrow$  optimal situation to use **Low Energy Theorems** to add higher order corrections.

QCD corrections dominant:



Difficult task since decay is already a loop effect.

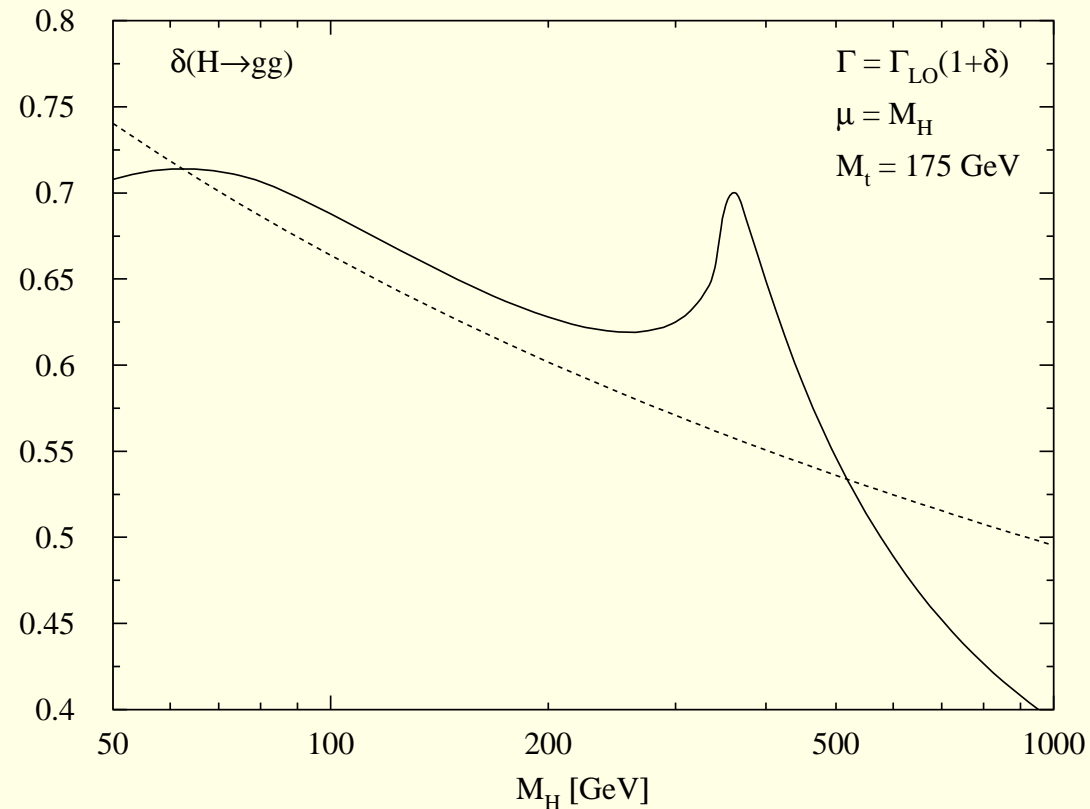
However, full massive calculation of  $\Gamma(H \rightarrow gg(q), q\bar{q}g)$  agrees with  $m_t \gg M_H$  result at 10%

$$\Gamma(H \rightarrow gg(q), q\bar{q}g) = \Gamma_{LO}(\alpha_s^{(N_L)}(M_H)) \left[ 1 + E^{(N_L)} \frac{\alpha_s^{(N_L)}}{\pi} \right]$$

$$E^{(N_L)} \xrightarrow{M_H^2 \ll 4m_q^2} \frac{95}{4} - \frac{7}{6}N_L$$

Dominant soft/collinear radiation do not resolve the Higgs boson coupling to gluons  $\longrightarrow$  QCD corrections are just a (big) rescaling factor

NLO QCD corrections almost 60 – 70% of LO result in the low mass region:



solid line  $\longrightarrow$  full massive NLO calculation

dashed line  $\longrightarrow$  heavy top limit ( $M_H^2 \ll 4m_t^2$ )

NNLO corrections calculated in the heavy top limit: add 20%

$\longrightarrow$  perturbative stabilization.

## Low-energy theorems, in a nutshell.

- **Observing that:**

In the  $p_H \rightarrow 0$  limit: the interactions of a Higgs boson with the SM particles arise by substituting

$$M_i \longrightarrow M_i \left( 1 + \frac{H}{v} \right) \quad (i = f, W, Z)$$

In practice: Higgs taken on shell ( $p_H^2 = M_H^2$ ), and limit  $p_H \rightarrow 0$  is limit of small Higgs masses (e.g.:  $M_H^2 \ll 4m_t^2$ ).

- **Then**

$$\lim_{p_H \rightarrow 0} \mathcal{A}(X \rightarrow Y + H) = \frac{1}{v} \sum_i M_i \frac{\partial}{\partial M_i} \mathcal{A}(X \rightarrow Y)$$

very convenient!

- Equivalent to an **Effective Theory** described by:

$$\mathcal{L}_{eff} = \frac{\alpha_s}{12\pi} G^{a\mu\nu} G_{\mu\nu}^a \frac{H}{v} (1 + O(\alpha_s))$$

including higher order QCD corrections.

For completeness:

$$\Gamma(H \rightarrow \gamma\gamma) = \frac{G_F \alpha^2 M_H^3}{128\sqrt{2}\pi^3} \left| \sum_f N_{cf} e_f^2 A_f^H(\tau_f) + A_W^H(\tau_W) \right|^2$$

where  $f(\tau)$  as in  $H \rightarrow gg$ :

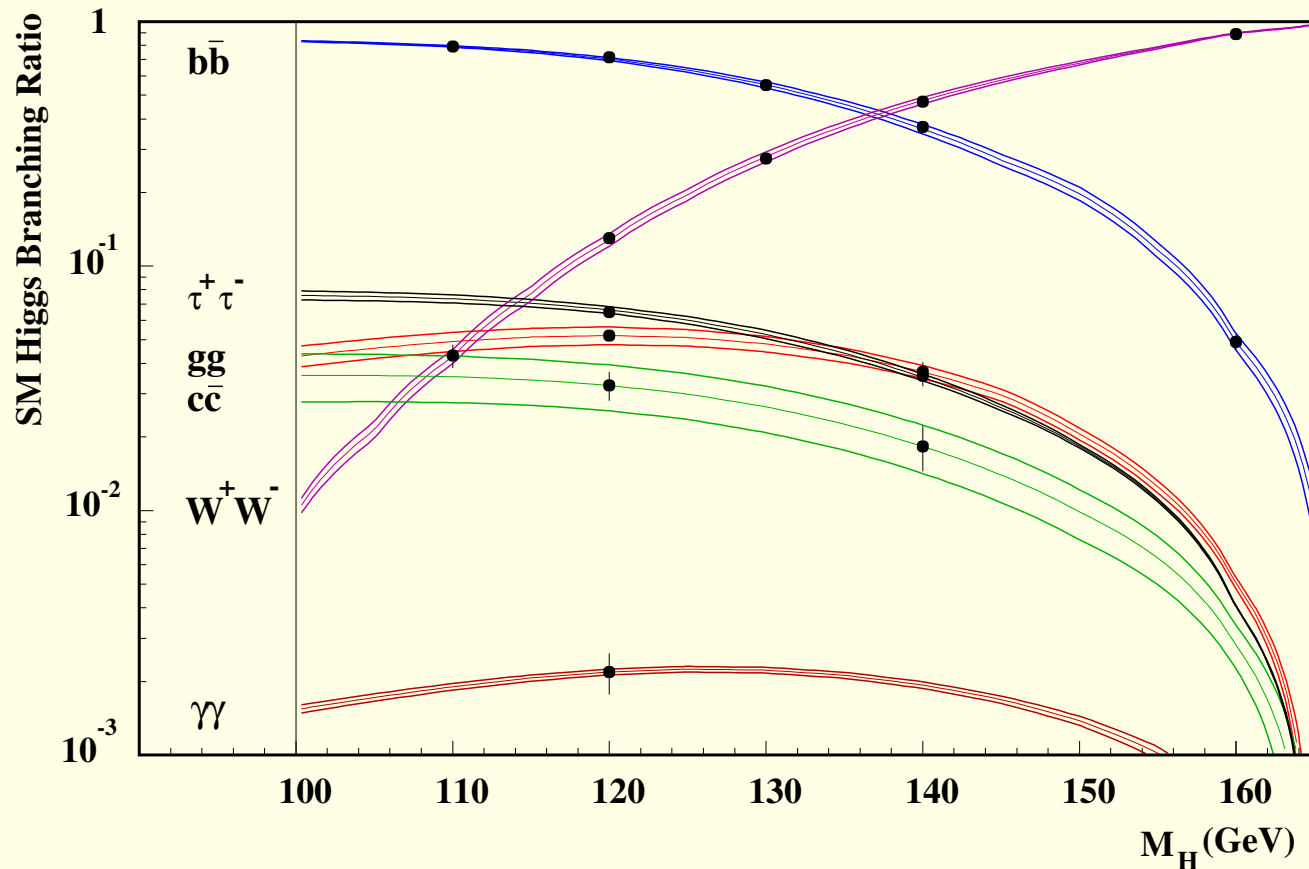
$$\begin{aligned} A_f^H &= 2\tau [1 + (1 - \tau)f(\tau)] \\ A_W^H(\tau) &= -[2 + 3\tau + 3\tau(2 - \tau)f(\tau)] \end{aligned}$$

$$\Gamma(H \rightarrow Z\gamma) = \frac{G_F^2 M_W^2 \alpha M_H^3}{64\pi^4} \left(1 - \frac{M_Z^2}{M_H^2}\right)^3 \left| \sum_f A_f^H(\tau_f, \lambda_f) + A_W^H(\tau_W, \lambda_W) \right|^2$$

where the form factors  $A_f^H(\tau, \lambda)$  and  $A_W^H(\tau, \lambda)$  can be found in the literature (see, e.g., M. Spira, hep-ph/9705337).

For both decays, both QCD and EW corrections are very small ( $\simeq 1 - 3\%$ ).

# Present theoretical accuracy on SM Higgs branching ratios



Example:  $M_H = 120$  GeV

Decay mode:	$b\bar{b}$	$WW^*$	$\tau^+\tau^-$	$c\bar{c}$	$gg$	$\gamma\gamma$
Theory	1.4%	2.3%	2.3%	23%	5.7%	2.3%

Mainly due to: pole masses  $m_c$  and  $m_b$ , and  $\alpha_s(\mu)$ .