

# Typos, Errata and Additions

## Essential Graduate Electrodynamics

### Lecture Notes

### Bernd Berg, Fall 2016

**p.11:** After equation (1.38):

By reasons that will become clear in the later physical interpretation the variable  $\zeta$  is called *rapidity*. For each value of  $d$  there is precisely one value of  $\zeta$  and vice versa, because the hyperbolic sine performs a one to one mapping. Such a function is called *isomorphic* in calculus.

...

Using finally  $\begin{pmatrix} x^0 \\ x^1 \end{pmatrix} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$  yields

$$\begin{aligned} 0 &= [\cosh(\zeta) - \sinh(\eta)]^2 - [-\sinh(\zeta) + \cosh(\eta)]^2 \\ &= -2 \cosh(\zeta) \sinh(\eta) + 2 \sinh(\zeta) \cosh(\eta) \\ &= -2 \tanh(\eta) + 2 \tanh(\zeta) \Rightarrow \zeta = \eta. \end{aligned} \quad (1.41)$$

**p.28:**

Consequently, we have

$$\lambda' = \lambda \sqrt{\frac{1+\beta}{1-\beta}} = \lambda \sqrt{\frac{\cosh \zeta + \sinh \zeta}{\cosh \zeta - \sinh \zeta}} = \lambda \exp(\zeta). \quad (1.130)$$

**p.70:**

$$Y_l^{-l} = \sqrt{\frac{(2l+1)(2l)!}{4\pi}} \frac{\sin^l \theta}{2^l l!} e^{-il\phi}. \quad (2.154)$$

**p.77:**

The traceless *quadrupole* tensor is defined by

$$Q^{ij} = Q_S^{ij} - Q_D^{ij} \text{ with } Q_S^{ij} = 3 \int x^i x^j \rho(\vec{x}') d^3 x', \quad Q_D^{ij} = \int r'^2 \delta^{ij} \rho(\vec{x}') d^3 x' \quad (3.10)$$

so that  $\sum_{i=1}^3 Q_S^{ii} = \sum_{i=1}^3 Q_D^{ii}$  holds.

**p.80:**

$$\Phi(\vec{x}) = \frac{\rho(\vec{x}')}{|\vec{x} - \vec{x}'|} + \frac{\vec{p}(\vec{x}') \cdot (\vec{x} - \vec{x}')}{|\vec{x} - \vec{x}'|^3}. \quad (3.22)$$

**p.101:***Faraday's Law* law of induction

$$\epsilon_{\text{emf}} = \oint_C (\vec{E} + \vec{\beta} \times \vec{B}) \cdot d\vec{l} = -\frac{1}{c} \frac{d}{dt} \Phi_m \quad \text{with} \quad \Phi_m = \int_S \vec{B} \cdot d\vec{a}, \quad (4.4)$$

**p.102:**

$$\nabla \cdot \vec{B} = 0, \quad (4.7)$$

which implies due to Gauss' theorem that the flux through a closed surface is zero.

**p.183:**

$$v_g = \frac{d\omega}{dk_q} = \frac{c}{\sqrt{\mu\epsilon}} \frac{d}{dk_q} \sqrt{k_q^2 + \gamma_q^2} = \frac{c}{\sqrt{\mu\epsilon}} \frac{k_q}{\sqrt{k_q^2 + \gamma_q^2}} < \frac{c}{\sqrt{\mu\epsilon}} \quad (6.48)$$

**p.190:**

$$\vec{E}_t = \frac{1}{2} (\vec{E}_t^+ + \vec{E}_t^-) = -\sin(kz) \frac{k}{\gamma^2} \nabla_t \psi(x, y) \quad (6.70)$$

**p.212:**

$$\vec{E}_{\text{in}} = \hat{\epsilon}_{\text{in}} E_{\text{in}} e^{ik_{\text{in}} \hat{k}_{\text{in}} \cdot \vec{x}}, \quad \vec{B}_{\text{in}} = \hat{k}_{\text{in}} \times \vec{E}_{\text{in}} \quad (7.87)$$

**p.242:**

The equation

$$\begin{aligned} 0 &= L_- Y_l^{-l} = L_- P_l^{-l} e^{-il\phi} \\ &= e^{-i\phi} \left( -\frac{\partial}{\partial \theta} + i \cot \theta \frac{\partial}{\partial \phi} \right) P_l^{-l} e^{-il\phi}, \end{aligned}$$

**p.256:**

(3) Show that

$$\begin{aligned} \epsilon_{\alpha\beta_1\gamma_1\delta_1} \epsilon^{\alpha\beta_2\gamma_2\delta_2} &= -\delta_{\beta_1}^{\beta_2} \delta_{\gamma_1}^{\gamma_2} \delta_{\delta_1}^{\delta_2} - \delta_{\beta_1}^{\gamma_2} \delta_{\gamma_1}^{\delta_2} \delta_{\delta_1}^{\beta_2} - \delta_{\beta_1}^{\delta_2} \delta_{\gamma_1}^{\beta_2} \delta_{\delta_1}^{\gamma_2} \\ &\quad + \delta_{\beta_1}^{\beta_2} \delta_{\gamma_1}^{\delta_2} \delta_{\delta_1}^{\gamma_2} + \delta_{\beta_1}^{\delta_2} \delta_{\gamma_1}^{\gamma_2} \delta_{\delta_1}^{\beta_2} + \delta_{\beta_1}^{\gamma_2} \delta_{\gamma_1}^{\beta_2} \delta_{\delta_1}^{\delta_2}. \end{aligned}$$

**p.285:**

(4) Use the limit of figure E.8 to calculate the principal value integral defined by

$$\begin{aligned} \frac{1}{2\pi i} P \int_{-\infty}^{\infty} dx \frac{f(x)}{x - \omega_R} &= \frac{1}{2\pi i} \lim_{\eta \rightarrow 0^+} \left[ \int_{-\infty}^{\omega_R - \eta} \frac{f(x) dx}{x - \omega_R} + \int_{\omega_R + \eta}^{+\infty} \frac{f(x) dx}{x - \omega_R} \right] \\ &= \frac{1}{2\pi i} \lim_{\eta \rightarrow 0^+} \left[ \int_{-\infty}^{\omega_R + i\eta - \eta} \frac{f(z) dz}{z - \omega_R - i\eta} + \int_{\omega_R + i\eta + \eta}^{+\infty} \frac{f(z) dz}{z - \omega_R - i\eta} \right] \end{aligned}$$