September 10, 2018 11:20

1

Special and General Relativity (PHZ 4601) Fall 2018 Solutions Set 3

6. Mössbauer precision for measuring a gravitational frequency shift (Rindler 1.9).

Let a 22 [m] long cabin fall freely in the gravitational field g and send a light signal from the top to the bottom. We need to show that when the light signal reaches the bottom, the cabin will already move with velocity $v > 10^{-5} [cm/s]$, so that the frequency shift can be detected. This is easily calculated.

Duration of the signal:

$$t = \frac{22 \,[m]}{3 \times 10^8 \,[m/s]} = 7.33 \times 10^{-8} \,[s] \,.$$

Velocity reached:

$$v = g t = (980 [cm/s]) \times (7.22 \times 10^{-8} [s]) = 7.2 \times 10^{-5} [cm/s].$$