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## Special and General Relativity (PHZ 4601/5606) Fall 2018 Solutions Set 8

## 20. Distance in a saddle.

For y = 0 we have  $z = x^2$  and, therefore, along the curve

$$ds^{2} = df^{2} + dx^{2} = (2x \, dx)^{2} + dx^{2} = (4x^{2} + 1) \, dx^{2}$$

With  $ds' = \sqrt{4x'^2 + 1} dx'$  we integrate then

$$s = \int_0^s ds' = \int_0^x \sqrt{4x'^2 + 1} \, dx' = \frac{x}{2} \sqrt{4x^2 + 1} + \frac{1}{4} \ln\left(\sqrt{4x^2 + 1} + 2x\right) \,,$$

where the integration was done with the online integral calculator from Mathematica. By bisection of the function s(x) we obtain for s = 10 the value

x = 3.041.