

Plot for assignment 24 set 7.

Calculation of r_{\min} defined by $U_{\text{eff}}^{\min} = U_{\text{eff}}(r_{\min})$:

$$U_{\rm eff}'(r) = \frac{\alpha}{r^2} - \frac{L^2}{\mu \, r^3}$$

$$0 = \alpha - \frac{L^2}{\mu \, r^{\rm min}}$$

$$r^{\rm min} = \frac{L^2}{\alpha \, \mu} = 1 \ \ {\rm for} \ \ \alpha = \mu = L = 1 \ .$$

The orbit is a circle with radius $r^{\min} = 1$.