

**ADVANCED DYNAMICS — PHY 4241/5227**  
**SOLUTIONS – SET 13**

Problem 49: Momentum conservation in the rest frame ( $m$  rest mass):

$$c \, dm = m \, g \, d\tau .$$

Separation of variables gives (with initial mass  $m_0$ ):

$$\int_{m_0}^{m(\tau)} = -\frac{g}{c} \int_0^\tau d\tau' \quad \Rightarrow \quad m(\tau) = m_0 e^{-g\tau/c} .$$

After  $\tau = 20$  years:

$$m(20 \text{ y}) = 1.09 \times 10^{-9} m_0 .$$

End of spacetrrip journey.