

ADVANCED DYNAMICS — PHY 4241/5227

HOME AND CLASS WORK – SET 1

(January 5, 2011)

- (1) Consider light passing from medium 1 into medium 2. Use Fermat's principle to derive Snell's law between the velocities of light, v_1 and v_2 , in two media and the angles of refraction, θ_1 and θ_2 (a figure will be given in class). Due in class (10 points).
- (2) Method of 2D projections for spherical coordinates. Each of the following tasks counts one point. Follow the instructions given in class (no other methods).
 1. Write x, y in cylindrical coordinates ρ, ϕ .
 2. Write $dx^2 + dy^2$ in cylindrical coordinates.
 3. Write cylindrical coordinates ρ, z in spherical coordinates r, θ .
 4. Write $d\rho^2 + dz^2$ in spherical coordinates.
 5. Write $dx^2 + dy^2 + dz^2$ in spherical coordinates.
 6. Write v^2 , the velocity squared, in cartesian coordinates.
 7. Write v^2 , in cylindrical coordinates.
 8. Write v^2 , in spherical coordinates.

Due January 12 before class (up to 8 points).

- (3) Read Landau-Lifshitz up to page 10 and the Handout, the first nine pages of "The Principle of Least Action" from Chapter 19 of *The Feynman Lectures on Physics*, Vol. II. Prepare questions about anything you do not understand. Due January 7 before class.
- (4) Write down your expectations for this course. What are the main objectives? How do they relate to your present knowledge? Due January 10 before class. Be detailed (up to 8 points)!
- (5) Consider a particle of mass $m = 1$, moving from $x_1 = 0$ at time $t_1 = 0$ to $x_2 = 1$ at time $t_2 = \pi/2$, under the influence of a one-dimensional harmonic potential of the form $V(x) = x^2/2$.
 1. Using Newton's equations of motion, obtain the time-dependent motion of the system; *i.e.*, solve for $x(t)$. Compute the action for this exact path.
 2. Using an approximate linear path of the form $x(t) = a + bt$, compute the action for this path and compare it with the value obtained before. Hint: Make sure that the path is consistent with the boundary conditions.
 3. Assume that the action result of (2.) is in units $J \cdot s$ and express it in multiples of $\hbar = 1.05 \times 10^{-34} J \cdot s$.

Due January 10 before class (10 points).