

ADVANCED DYNAMICS — PHY 4241/5227

HOME AND CLASS WORK – SET 6

(February 9, 2011)

Read Landau-Lifshitz §15. Due February 11.

(18) Consider the effective potential of the Kepler problem

$$U_{\text{eff}}(r) = -\frac{\alpha}{r} + \frac{L^2}{2\mu r^2} .$$

(A) Calculate the value  $r_0^{\text{min}}$  where  $U_{\text{eff}}(r)$  has its minimum.

(B) Calculate  $U_{\text{eff}}^{\text{min}} = U_{\text{eff}}(r_0^{\text{min}})$ .

(C) Assume an energy  $E < 0$  and calculate the values of the turning points  $r_{\text{min}}$  and  $r_{\text{max}}$ .

Due in class, 4 points.

(19) Assume  $0 < e < 1$  for the eccentricity and transform the elliptic equation

$$\frac{p}{r} = 1 + e \cos(\phi), \quad p > 0 \quad \text{into the form} \quad \frac{x'^2}{a^2} + \frac{y'^2}{b^2} = 1 .$$

This means, *derive* the definitions of  $x'$ ,  $y'$ , major half-axis  $a$  and minor half-axis  $b$  in terms of  $x$ ,  $y$ ,  $p$  and  $e$ . Due in class, 4 points.

(20) Use the inertial frame of §15 of the book and plot the orbits for the four initial conditions of the table in set 5 (best in one figure). Indicate the initial positions. Due February 18 before class, 12 points.