Solution for assignment 9a:

For a bilinear kinetic Energy we find by differentiation and carrying the sum over i out

$$\sum_{i} \dot{q}_{i} \frac{\partial T}{\partial \dot{q}_{i}} = \sum_{i} \dot{q}_{i} \frac{\partial}{\partial \dot{q}_{i}} \sum_{j,k} a_{jk} \dot{q}_{j} \dot{q}_{k} = \sum_{i,j,k} \dot{q}_{i} \left(\delta_{ij} \dot{q}_{k} + \dot{q}_{j} \delta_{ik} \right)$$

$$= \sum_{j,k} a_{jk} \left(\dot{q}_{j} \dot{q}_{k} + \dot{q}_{j} \dot{q}_{k} \right) = 2T.$$

Solution for assignment 9b: Motivation of generalized momentum definition.

$$\frac{\partial}{\partial \dot{x}_i} \left(\frac{1}{2} \, m \, \vec{v}^2 - V(\vec{x}) \right) = m \, \dot{x}_i = p_i .$$