

Mathematical Physics — PHZ 3113

Homework 9 (March 25, 2013)

Jacobi Determinant

1. Calculate

$$I = \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} dx dy e^{-(x-y)^2 - (x+y)^2}.$$

2. Calculate

$$I = \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} dx_1 dx_2 dx_3 \\ e^{-(x_1+x_2+x_3)^2 - (x_1+x_2-x_3)^2 - (x_1-x_2-x_3)^2}.$$