

# Higgs Boson Physics, Part IV

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TASI 2004, Boulder

# Outline of Part IV

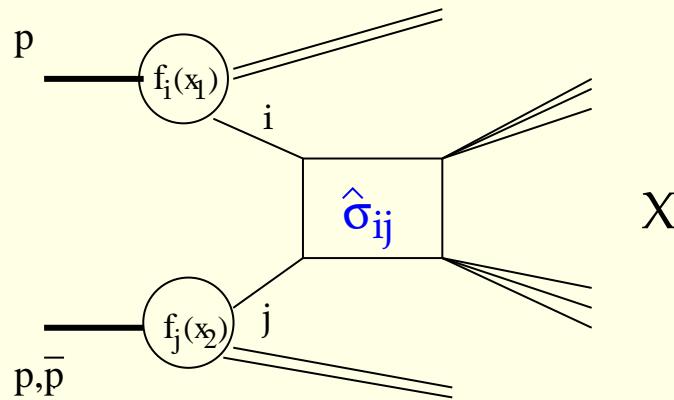
- The current status of theoretical predictions in Higgs physics:  
*How does theory compare to experiments?*
- Highlights from the *theoretical activity* of the last few years:
  - $gg \rightarrow H$ : gluon-gluon fusion calculated at NNLO in QCD, consolidating the reliability of a very difficult theoretical prediction.
  - $q\bar{q}, gg \rightarrow t\bar{t}H$  calculated at NLO in QCD, stabilizing an important theoretical prediction for Higgs discovery in the (most interesting) low mass region.
  - $q\bar{q}, gg \rightarrow b\bar{b}H, bg \rightarrow bH, b\bar{b} \rightarrow H$ : now available including NLO (NNLO) QCD corrections, which clarify a very controversial theoretical scenario.
- Final Overview

Understanding the current status of theoretical  
predictions

or

How theory can compare to experiments

The basic picture of a  $p\bar{p}, pp \rightarrow X$  high energy process . . .



where the short and long distance part of the QCD interactions can be factorized and the cross section for  $pp, p\bar{p} \rightarrow X$  can be calculated as:

$$\sigma(pp, p\bar{p} \rightarrow X) = \sum_{ij} \int dx_1 dx_2 f_i^p(x_1) f_j^{p,\bar{p}}(x_2) \hat{\sigma}(ij \rightarrow X)$$

- $ij \rightarrow$  quarks or gluons (partons)
- $f_i^p(x), f_i^{p,\bar{p}}(x)$ : Parton Distributions Functions: probability densities (probability of finding parton  $i$  in  $p$  or  $\bar{p}$  with a fraction  $x$  of the original hadron momentum)
- $\hat{\sigma}(ij \rightarrow X)$ : partonic cross section

... is complicated by the presence of interactions

- Focus on strong interactions, dominant at hadron colliders
- In the  $ij \rightarrow X$  process, initial and final state partons radiate and absorb gluons/quarks:

How to calculate the physical cross section?

- Due to the very same interactions: the strong coupling constant ( $\alpha_s = g_s^2/4\pi$ ) becomes a function of the energy scale ( $Q^2$ ), such that

$\alpha_s(Q^2) \rightarrow 0$  for large scales  $Q^2$  : running coupling



we can calculate  $\hat{\sigma}(ij \rightarrow X)$  perturbatively

$$\hat{\sigma}(ij \rightarrow X) = \alpha_s^k \sum_{m=0}^n \hat{\sigma}_{ij}^{(m)} \alpha_s^m$$

n=0 : Leading Order (LO), or tree level or Born level

n=1 : Next to Leading Order (NLO), include  $O(\alpha_s)$  corrections

.....

## Perturbative approach and scale dependence

- At each order in  $\alpha_s$  the expression of  $\hat{\sigma}(ij \rightarrow X)$  contains infinities that are canceled by a subtraction procedure: renormalization.
- A remnant of the subtraction point is left at each perturbative order as a renormalization scale dependence ( $\mu_R$ )

$$\hat{\sigma}(ij \rightarrow X) = \alpha_s^k(\mu_R) \sum_{m=0}^n \hat{\sigma}_{ij}^{(m)}(\mu_R, Q^2) \alpha_s^m(\mu_R)$$

- A similar approach introduces a subtraction point dependence in the initial state parton densities: factorization scale dependence ( $\mu_F$ )

Setting  $\boxed{\mu_R = \mu_F = \mu}$  :

$$\sigma(pp, p\bar{p} \rightarrow X) = \sum_{ij} \int dx_1 dx_2 f_i^p(x_1, \mu) f_j^{p, \bar{p}}(x_2, \mu) \sum_{m=0}^n \hat{\sigma}_{ij}^{(m)}(\mu, Q^2) \alpha_s^{m+k}(\mu)$$

The theoretical error is systematically organized as an expansion in  $\alpha_s$

## Ex.: General structure of a NLO calculation

NLO total cross section:

$$\sigma_{p\bar{p},pp}^{NLO} = \sum_{i,j} \int dx_1 dx_2 \mathcal{F}_i^p(x_1, \mu_F) \mathcal{F}_j^{\bar{p},p}(x_2, \mu_F) \hat{\sigma}_{ij}^{NLO}(x_1, x_2, \mu_R, \mu_F)$$

where

$$\hat{\sigma}_{ij}^{NLO} = \hat{\sigma}_{ij}^{LO} + \frac{\alpha_s}{4\pi} \delta \hat{\sigma}_{ij}^{NLO}$$

NLO corrections made of:

$$\delta \hat{\sigma}_{ij}^{NLO} = \hat{\sigma}_{virt}^{ij} + \hat{\sigma}_{real}^{ij}$$

- $\hat{\sigma}_{virt}^{ij}$ : one loop virtual corrections.
- $\hat{\sigma}_{real}^{ij}$ : one gluon/quark real emission.
- use  $\alpha_s^{NLO}(\mu)$  and match with NLO PDF's.

→ renormalize UV divergences ( $d=4 - 2\epsilon_{UV}$ )

→ cancel IR divergences in  $\hat{\sigma}_{virt} + \hat{\sigma}_{real}$  ( $d=4 - 2\epsilon_{IR}$ )

→ check  $\mu$ -dependence of  $\sigma_{p\bar{p},pp}^{NLO}(\mu_R, \mu_F)$

## Some important facts . . .

- In hadronic production modes QCD effects can be very large.
- Tree level or Leading Order (LO) cross sections normally have very large uncertainties due to:
  - ▷ renormalization/factorization scale dependence
  - ▷ uncertainties from PDF's
- Differential cross sections very sensitive to higher order QCD corrections.
- Main modes have very large QCD background. Realistic studies, including higher order QCD corrections, are vital to a correct estimate of the background.



Crucial to know Higher Order QCD corrections

## Some References for Part IV

State-of-the-art of QCD predictions for Higgs production at Hadron Colliders.

process	$\sigma_{NLO,NNLO}$ by
$gg \rightarrow H$	S.Dawson, NPB 359 (1991), A.Djouadi, M.Spira, P.Zerwas, PLB 264 (1991) C.J.Glosser <i>et al.</i> , JHEP (2002); V.Ravindran <i>et al.</i> , NPB 634 (2002) D. de Florian <i>et al.</i> , PRL 82 (1999) R.Harlander, W.Kilgore, PRL 88 (2002) ( <b>NNLO</b> ) C.Anastasiou, K.Melnikov, NPB 646 (2002) ( <b>NNLO</b> ) V.Ravindran <i>et al.</i> , NPB 665 (2003) ( <b>NNLO</b> ) S.Catani <i>et al.</i> JHEP 0307 (2003) ( <b>NNLL</b> ), G.Bozzi <i>et al.</i> , PLB 564 (2003)
$q\bar{q} \rightarrow (W,Z)H$	T.Han, S.Willenbrock, PLB 273 (1991) O.Brien, A.Djouadi, R.Harlander, PLB 579 (2004) ( <b>NNLO</b> )
$q\bar{q} \rightarrow q\bar{q}H$	T.Han, G.Valencia, S.Willenbrock, PRL 69 (1992) T.Figy, C.Oleari, D.Zeppenfeld, PRD 68 (2003)
$q\bar{q}, gg \rightarrow t\bar{t}H$	W.Beenakker <i>et al.</i> , PRL 87 (2001), NPB 653 (2003) S.Dawson <i>et al.</i> , PRL 87 (2001), PRD 65 (2002), PRD 67,68 (2003)
$q\bar{q}, gg \rightarrow b\bar{b}H$	S.Dittmaier, M.Krämer, M.Spira, hep-ph/0309204 S.Dawson <i>et al.</i> , PRD 69 (2004)
$gb(\bar{b}) \rightarrow b(\bar{b})H$	J.Cambell <i>et al.</i> , PRD 67 (2003)
$b\bar{b}H$	D.A.Dicus <i>et al.</i> PRD 59 (1999); C.Balasz <i>et al.</i> , PRD 60 (1999). R.Harlander, W.Kilgore, PRD 68 (2003) ( <b>NNLO</b> )

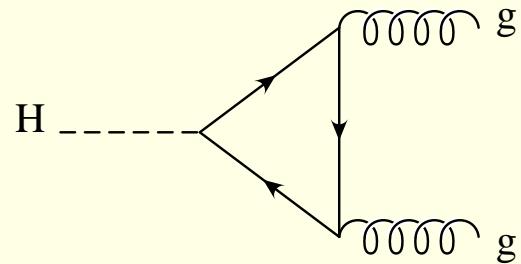
## Highlights of recent theoretical activity

- ▷  $H \rightarrow gg$  at NNLO+NNLL
- ▷  $p\bar{p}, pp \rightarrow t\bar{t}H$  at NLO
- ▷  $p\bar{p}, pp \rightarrow b\bar{b}H$  at NLO

Apologies for what will be omitted ...

Preliminaries : Higher order corrections  $\Gamma(H \rightarrow gg)$

Start from tree level:



$$\Gamma(H \rightarrow gg) = \frac{G_F \alpha_s^2 M_H^3}{36\sqrt{2}\pi^3} \left| \sum_q A_q^H(\tau_q) \right|^2$$

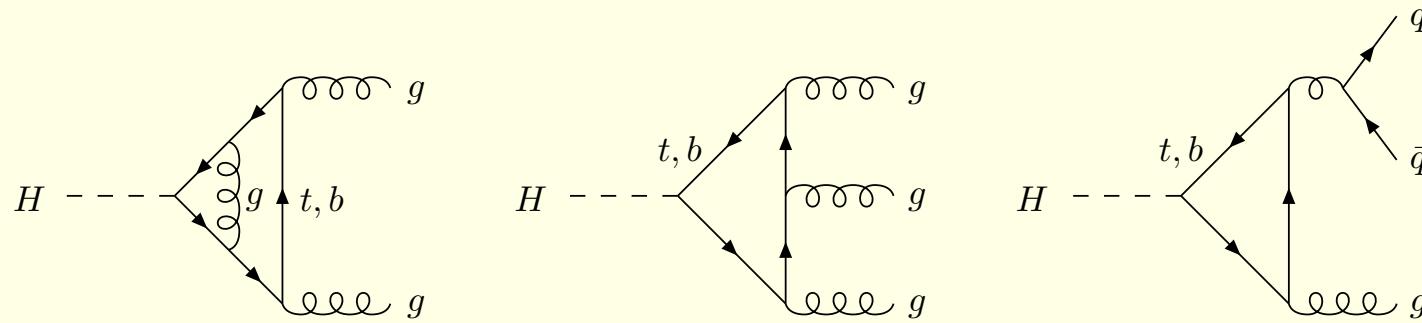
where  $\tau_q = 4m_q^2/M_H^2$  and

$$A_q^H(\tau) = \frac{3}{2}\tau [1 + (1 - \tau)f(\tau)]$$

$$f(\tau) = \begin{cases} \arcsin^2 \frac{1}{\sqrt{\tau}} & \tau \geq 1 \\ -\frac{1}{4} \left[ \ln \frac{1+\sqrt{1-\tau}}{1-\sqrt{1-\tau}} - i\pi \right]^2 & \tau < 1 \end{cases}$$

Main contribution from top quark  $\rightarrow$  optimal situation to use  
Low Energy Theorems to add higher order corrections.

QCD corrections dominant:



Difficult task since decay is already a loop effect.

However, full massive calculation of  $\Gamma(H \rightarrow gg(q), q\bar{q}g)$  agrees with  $m_t \gg M_H$  result at 10%

$$\Gamma(H \rightarrow gg(q), q\bar{q}g) = \Gamma_{LO}(\alpha_s^{(N_L)}(M_H)) \left[ 1 + E^{(N_L)} \frac{\alpha_s^{(N_L)}}{\pi} \right]$$

$$E^{(N_L)} \xrightarrow{M_H^2 \ll 4m_q^2} \frac{95}{4} - \frac{7}{6} N_L$$

Dominant soft/collinear radiation do not resolve the Higgs boson coupling to gluons  $\longrightarrow$  QCD corrections are just a (big) rescaling factor

## Low-energy theorems, in a nutshell.

- Observing that:

In the  $p_H \rightarrow 0$  limit: the interactions of a Higgs boson with the SM particles arise by substituting

$$M_i \longrightarrow M_i \left( 1 + \frac{H}{v} \right) \quad (i = f, W, Z)$$

In practice: Higgs taken on shell ( $p_H^2 = M_H^2$ ), and limit  $p_H \rightarrow 0$  is limit of small Higgs masses (e.g.:  $M_H^2 \ll 4m_t^2$ ).

- Then

$$\lim_{p_H \rightarrow 0} \mathcal{A}(X \rightarrow Y + H) = \frac{1}{v} \sum_i M_i \frac{\partial}{\partial M_i} \mathcal{A}(X \rightarrow Y)$$

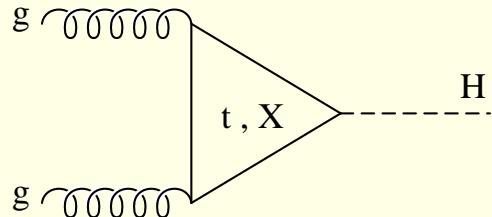
very convenient!

- Equivalent to an Effective Theory described by:

$$\mathcal{L}_{eff} = \frac{\alpha_s}{12\pi} G^{a\mu\nu} G^a_{\mu\nu} \frac{H}{v} (1 + O(\alpha_s))$$

including higher order QCD corrections.

# $gg \rightarrow H$ , the leading production mode

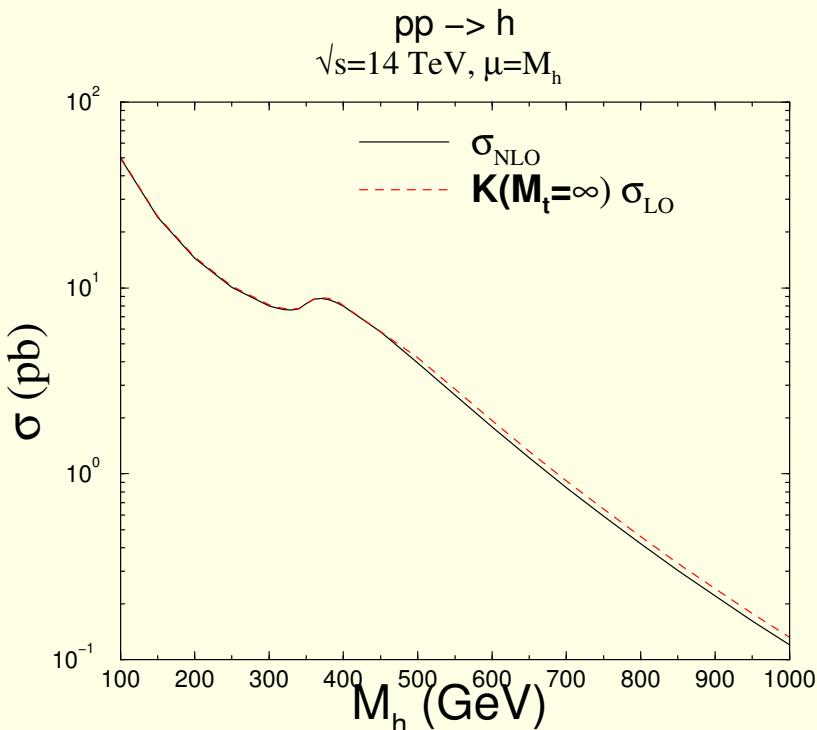


$$\sigma_{LO} = \frac{G_F \alpha_s(\mu)^2}{288\sqrt{2}\pi} \left| \sum_q A_q^H(\tau_q) \right|^2$$

$$\tau_q = 4m_q^2/M_H^2$$

$$A_q^H(\tau_q) \rightarrow 1 \text{ for } \tau_q \rightarrow \infty$$

NLO QCD corrections calculated exactly and in the  $m_t \rightarrow \infty$  limit.



where the  $K$ -factor is defined as:

$$K(m_t = \infty) = \lim_{m_t \rightarrow \infty} K = \lim_{m_t \rightarrow \infty} \frac{\sigma_{NLO}}{\sigma_{LO}}$$

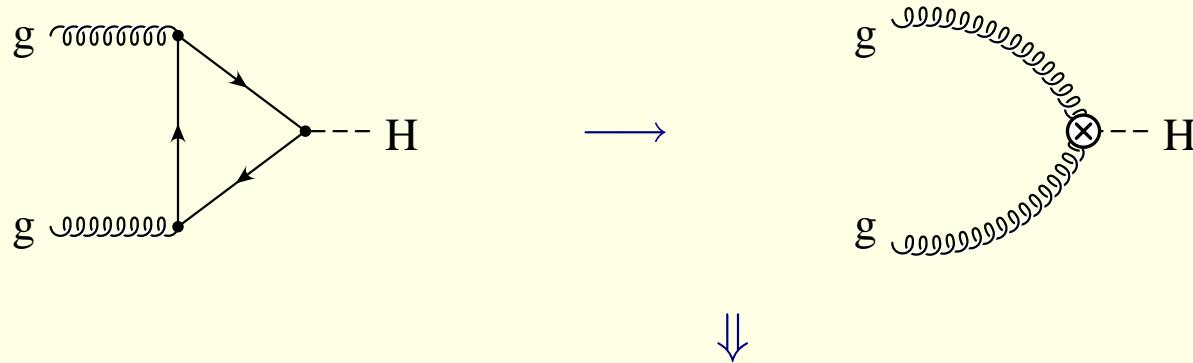
perfect agreement even for  $M_H \gg m_t$



soft radiation dominates

As for  $H \rightarrow gg$ , this suggest to use at NNLO:

→ low energy theorems ( $m_t \rightarrow \infty$ )



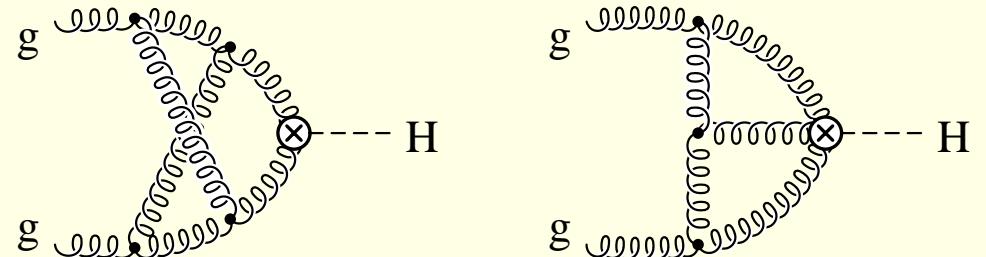
$$\mathcal{L}_{eff} = \frac{H}{4v} C(\alpha_s) G^{a\mu\nu} G^a_{\mu\nu}$$

where, including NLO and NNLO QCD corrections:

$$C(\alpha_s) = \frac{1}{3} \frac{\alpha_s}{\pi} \left[ 1 + c_1 \frac{\alpha_s}{\pi} + c_2 \left( \frac{\alpha_s}{\pi} \right)^2 + \dots \right]$$

This reduces by one the order of loops.

Ex.: at NNLO  
 ↓  
 calculates 2-loop diagrams

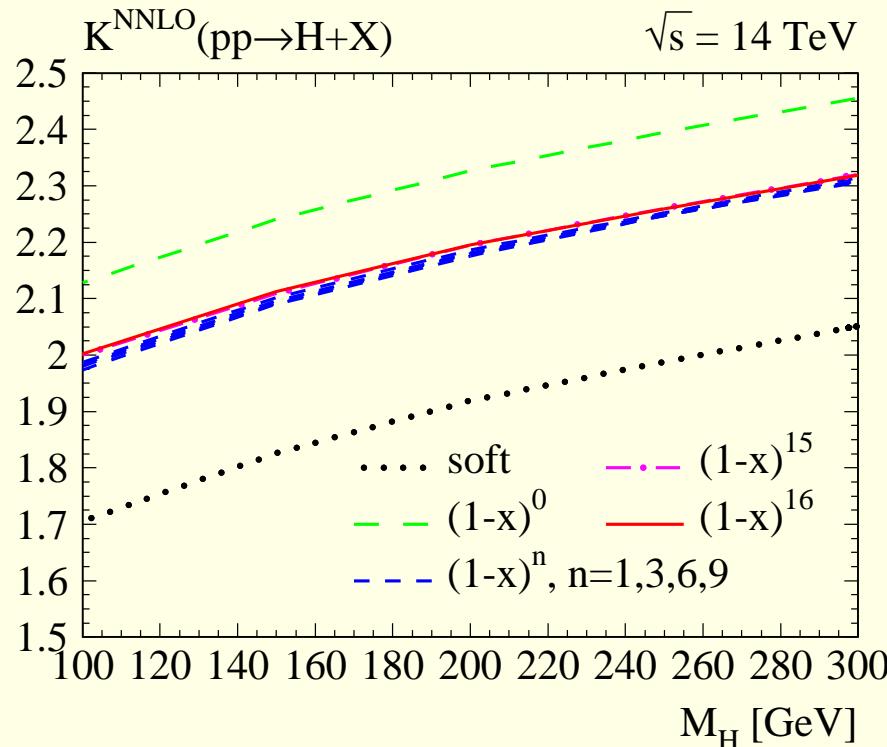


→ soft limit ( $x = M_H^2/\hat{s} \rightarrow 1$ ), where

$$\hat{\sigma}_{ij} = \sum_{n \geq 0} \left( \frac{\alpha_s}{\pi} \right)^n \hat{\sigma}_{ij}^{(n)}$$

is calculated as an expansion around the soft limit:

$$\hat{\sigma}_{ij}^{(n)} = \underbrace{a^{(n)} \delta(1-x) + \sum_{k=0}^{2n-1} b_k^{(n)} \left[ \frac{\ln^k(1-x)}{1-x} \right]_+}_{\text{purely soft terms}} + \underbrace{\sum_{l=0}^{\infty} \sum_{k=0}^{2n-1} c_{lk}^{(n)} (1-x)^l \ln^k(1-x)}_{\text{collinear+hard terms}}$$



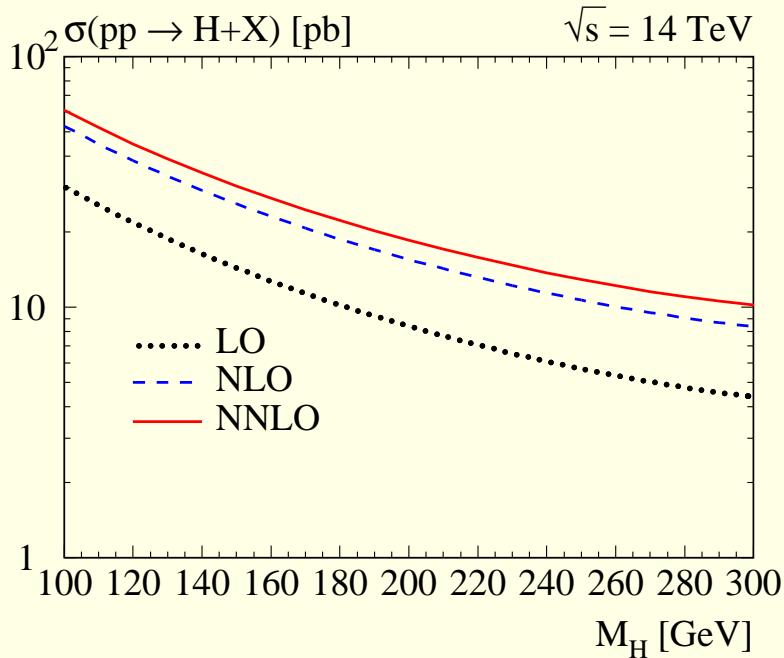
NNLO  $\longrightarrow a^{(2)}, b_k^{(2)}, c_{lk}^{(2)}$   
 (for  $l \geq 0$  and  $k=0, \dots, 3$ ).



**Remarkable convergence**

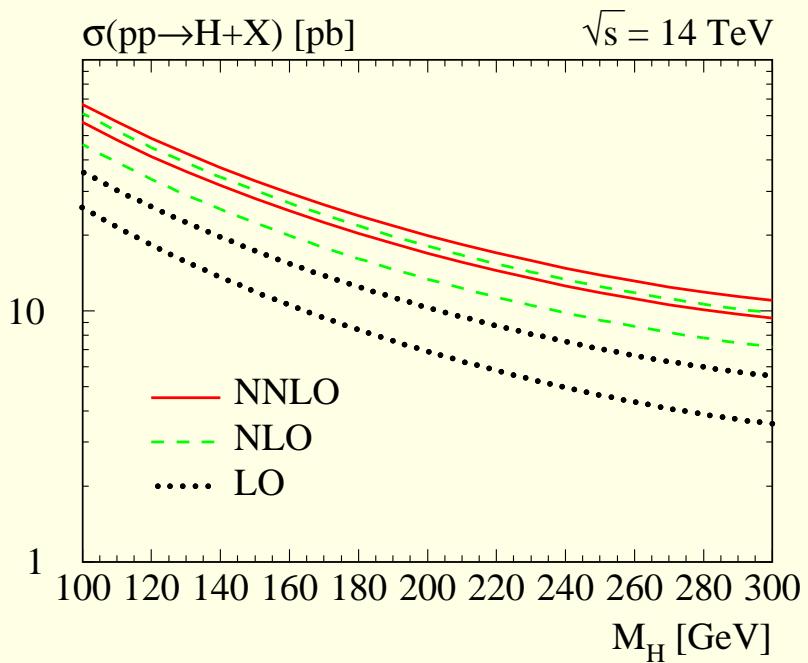
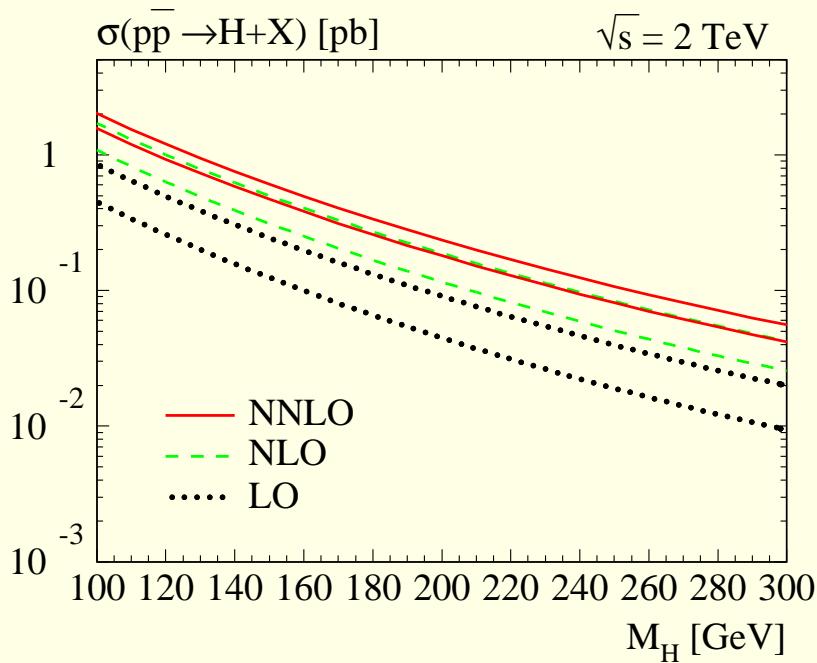
Confirmed by exact calculation.

# Dramatically improved perturbative behavior

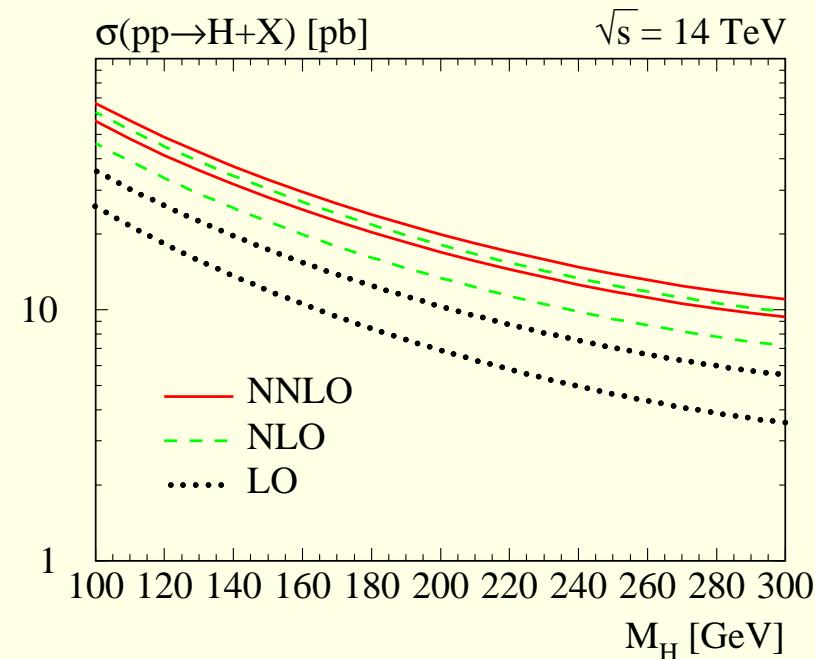
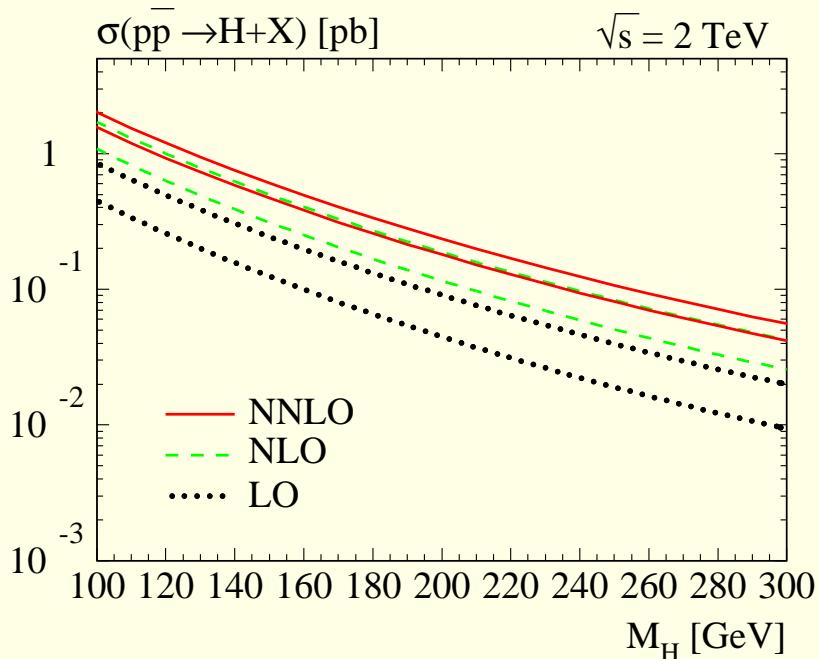
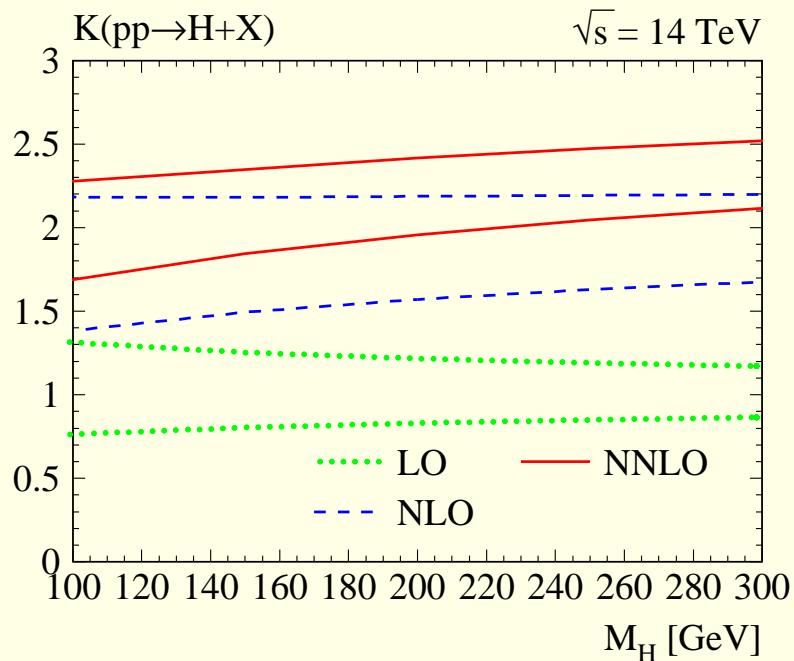
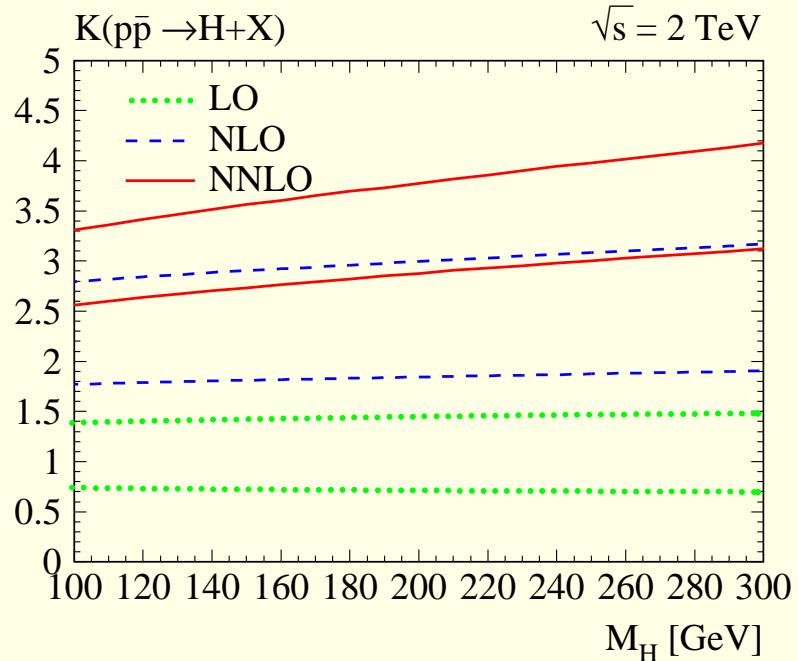


convergence in going:  
 $\text{LO} \longrightarrow \text{NLO} \longrightarrow \text{NNLO}$

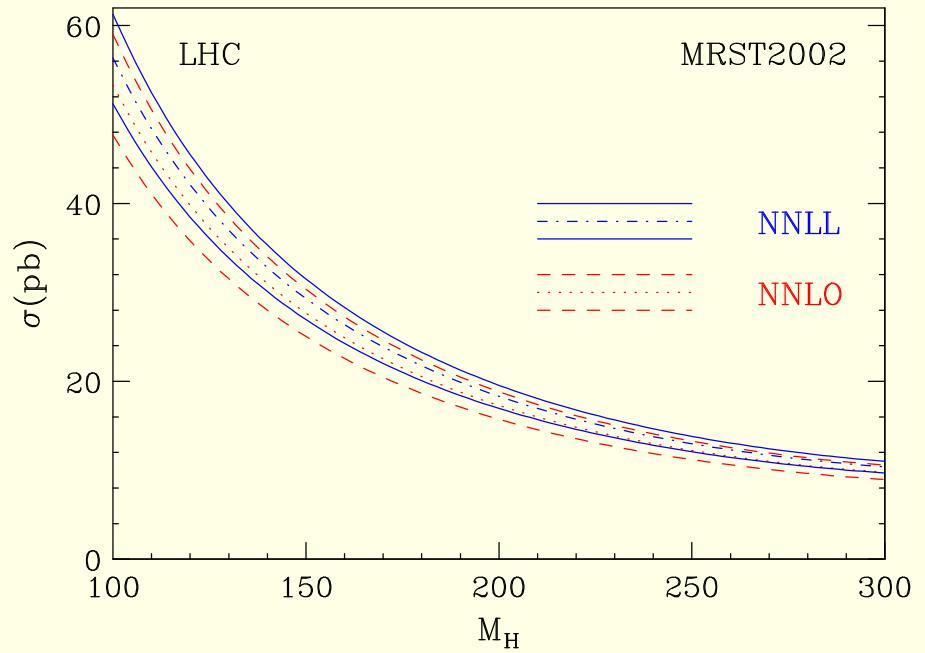
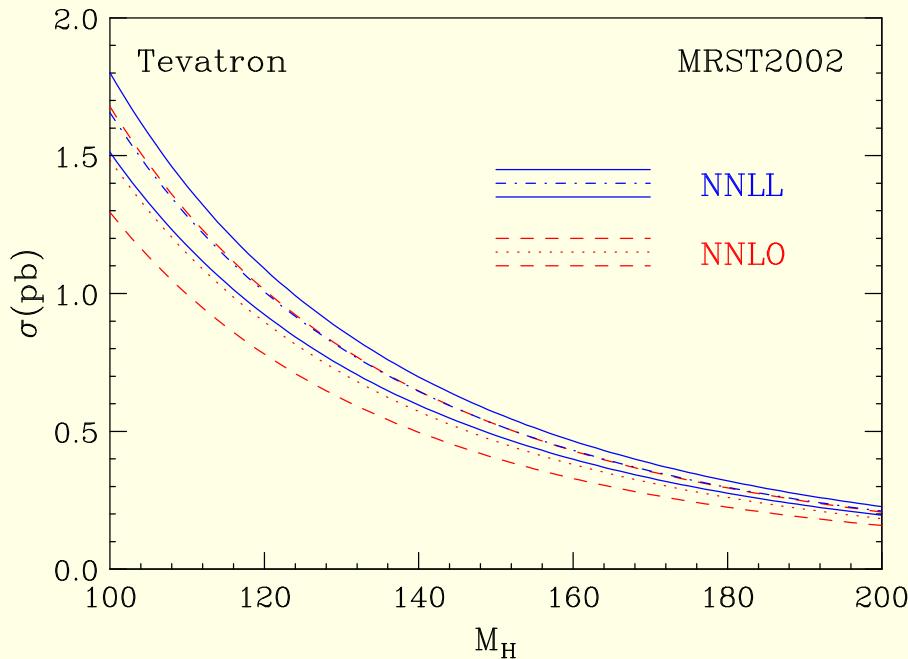
Confirmed by the full  
 $\mu_R/\mu_F$  dependence:



# A comment on K-factors ...



## Further improvement: resumming soft logs

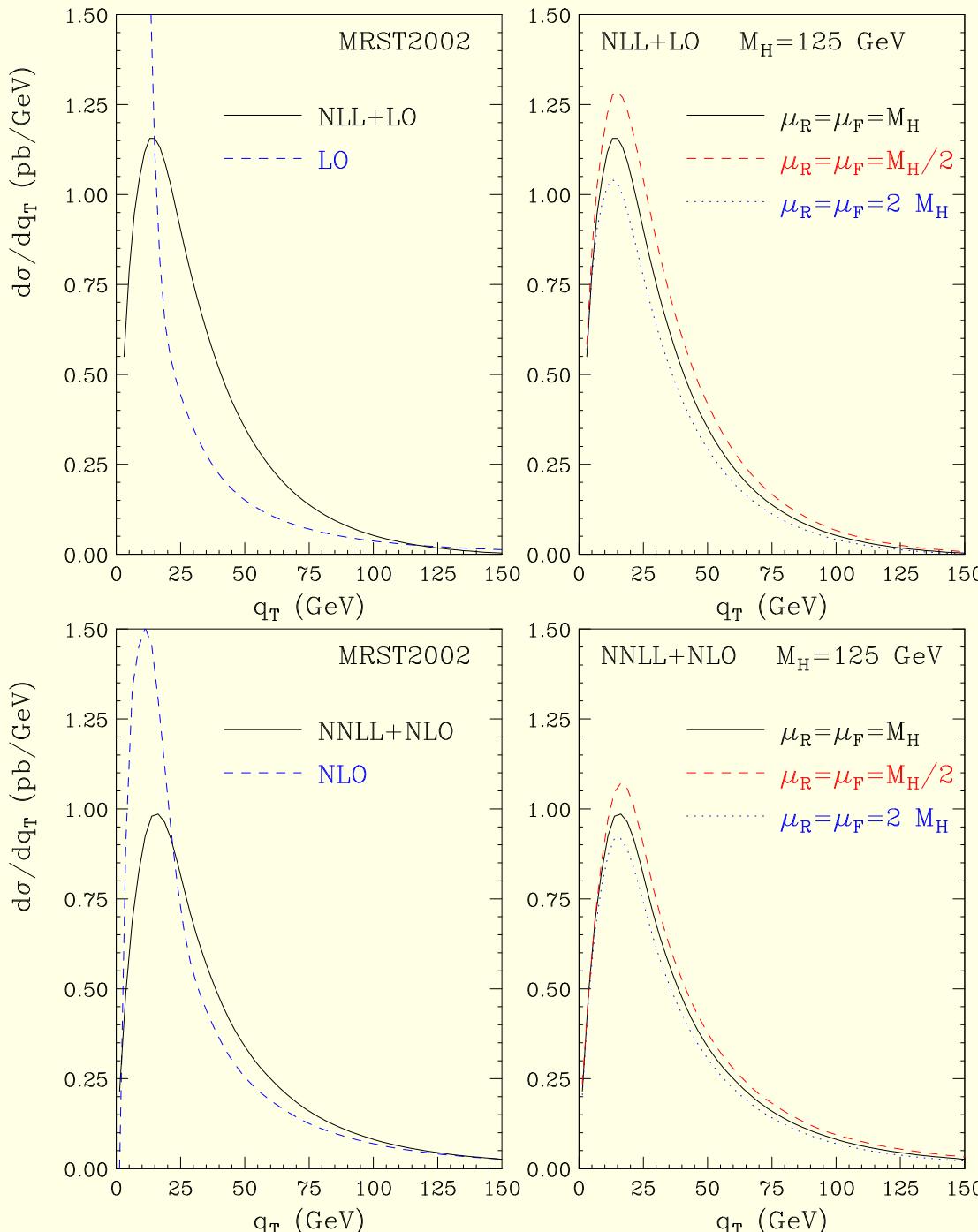


$$\sigma^{(res)}(s, M_H^2) = \underbrace{\sigma^{(SV)}(s, M_H^2)}_{\text{resummed}} + \sigma^{(\text{match})}(s, M_H^2)$$

with **NNLO+NNLL** : Theoretical uncertainty reduced to:

- $\simeq 10\%$  perturbative uncertainty, including the  $m_t \rightarrow \infty$  approximation.
- $\simeq 10\%$  from (now existing, but still to be tested) NNLO PDF's.

# Resummation crucial in transverse momentum distributions



$q_T \longrightarrow$  Higgs boson  
transverse momentum

large  $q_T$   $\xrightarrow{q_T > M_H}$   
perturbative expansion  
in  $\alpha_s(\mu)$

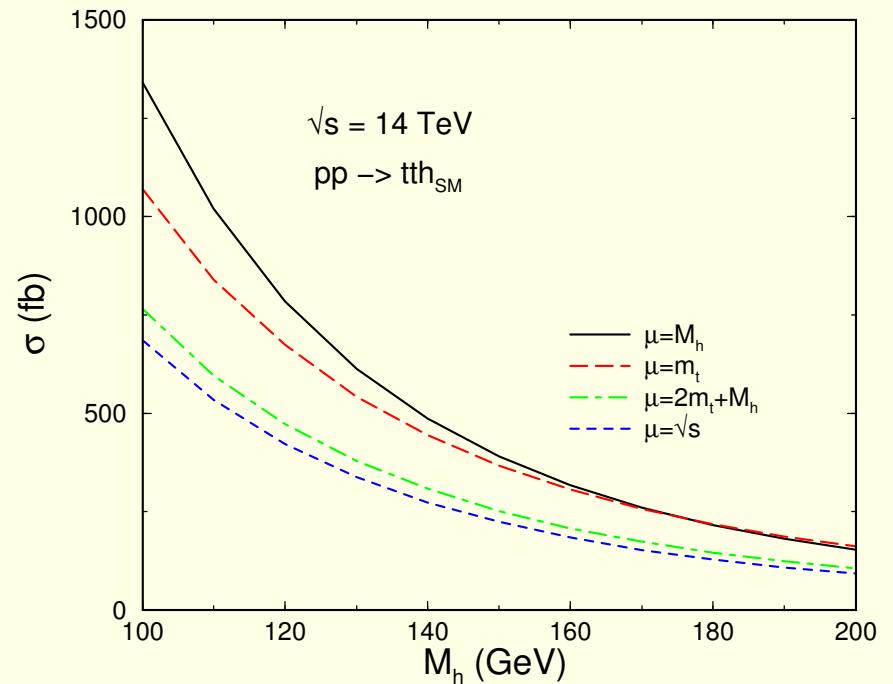
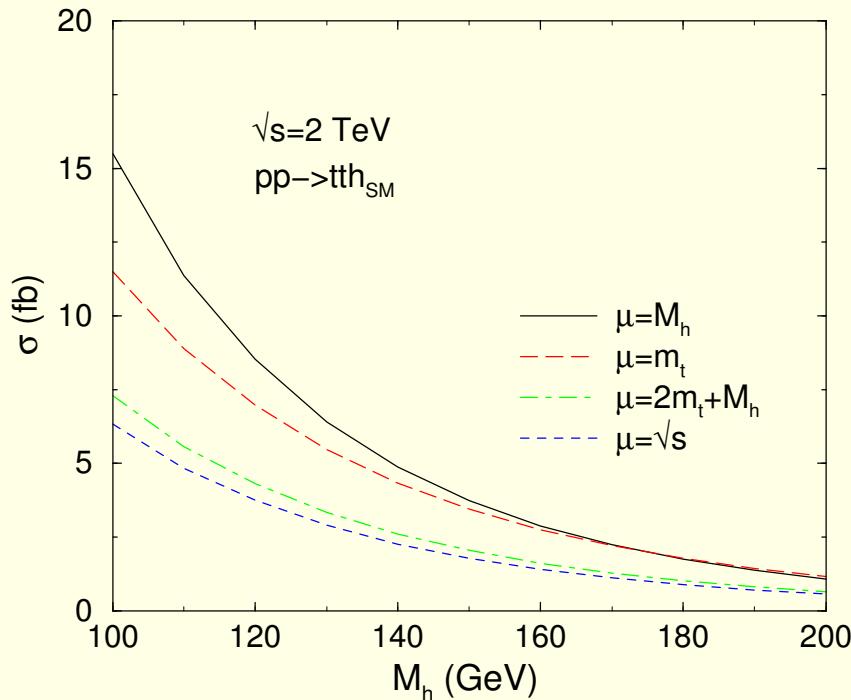
small  $q_T$   $\xrightarrow{q_T \ll M_H}$   
need to resum large  
 $\ln(M_H^2/q_T^2)$

# Higgs boson production with Heavy Quarks pairs: $p\bar{p}, pp \rightarrow t\bar{t}H, b\bar{b}H$

Last NLO calculation to be completed, mainly due to:

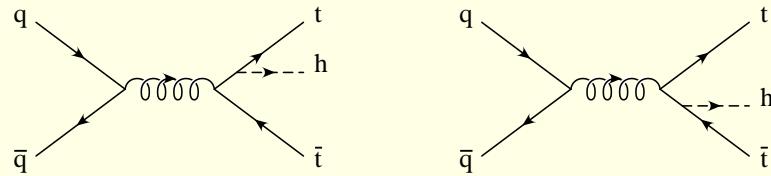
- many external particles ( $2 \rightarrow 3$  process)
- many massive particles

Still, NLO calculation badly needed: very strong  $\mu_R/\mu_F$  dependence at LO.

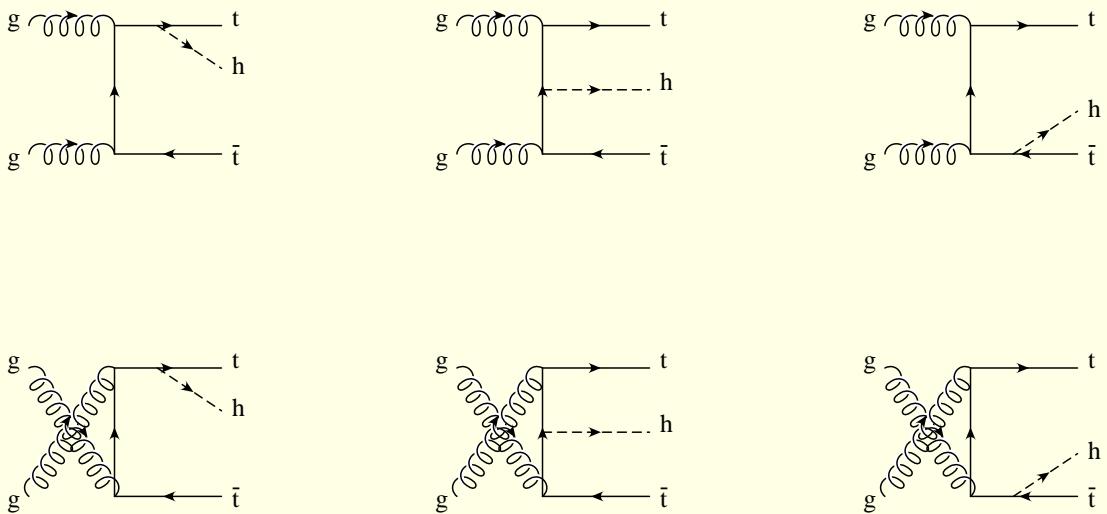


$p\bar{p}, pp \rightarrow t\bar{t}H$ : tree level

$q\bar{q} \rightarrow t\bar{t}H$   
leading  
contribution at  
the Tevatron

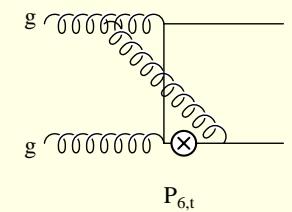
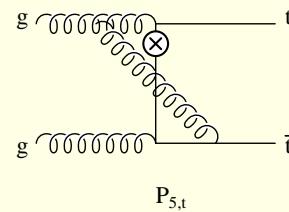
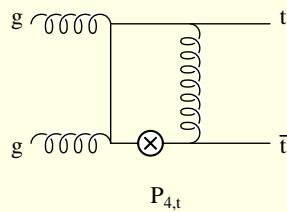
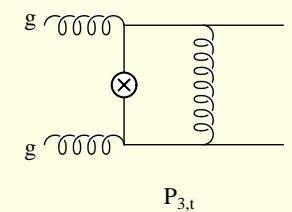
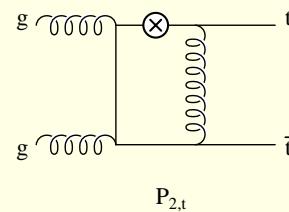
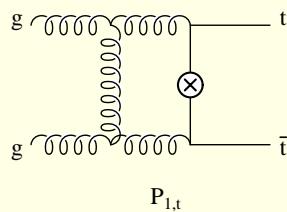


$gg \rightarrow t\bar{t}H$   
leading  
contribution at  
the LHC

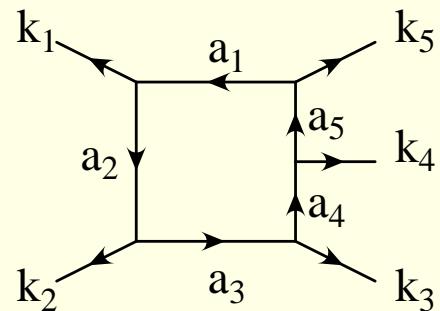


# $p\bar{p}, pp \rightarrow Q\bar{Q}H$ : $\mathcal{O}(\alpha_s)$ virtual corrections

Main challenge: Pentagon scalar and tensor integrals with several external and internal massive particles



- **Scalar pentagon integrals:** reduced to linear combination of five box scalar integrals ([Z.Bern,L.J.Dixon](#), D.A.Kosower; A.Denner)
- **Tensor pentagon integrals:** numerical instabilities (due to Gram determinant spurious singularities) treated both analytically and numerically.



gives origin to scalar integrals of the form:

$$E0 = \frac{1}{16\pi^2} (4\pi\mu^2)^\epsilon \Gamma(3+\epsilon) \int d^5 a_i \frac{\delta(1 - \sum_{i=1}^5 a_i)}{[\mathcal{D}(a_i)]^{3+\epsilon}}$$

where  $\mathcal{D}(a_i) = \sum_{i,j=1}^5 S_{ij} a_i a_j$

$$\left\{ \begin{array}{l} S_{ij} = \frac{1}{2} (M_i^2 + M_j^2 - p_{ij}) \\ p_{ij} = k_i + k_{i+1} + \cdots + k_{j-1} \end{array} \right.$$

scalar pentagon  $\longrightarrow$   $\sum$  scalar boxes

$$I_n = \frac{(-1)^n}{2} \left[ \sum_{i=1}^n c_i I_{n-1}^{(i)} + (n-5+2\epsilon) c_0 I_n^{6-2\epsilon} \right]$$

$\Downarrow$

$$E0 = -\frac{1}{2} \left[ \sum_{i=1}^5 c_i D0^{(i)} + 2\epsilon c_0 E0^{6-2\epsilon} \right]$$

Pentagon tensor integrals, e.g.:

$$\begin{aligned} E_1^\mu &= E_1^{(1)} p_1^\mu + E_1^{(2)} p_2^\mu + E_1^{(3)} p_3^\mu + E_1^{(4)} p_4^\mu \\ E_2^{\mu\nu} &= E_2^{(11)} p_1^\mu p_1^\nu + \dots + E_2^{(12)} (p_1^\mu p_2^\nu + p_1^\nu p_2^\mu) + \dots \\ E_3^{\mu\nu\rho} &= \dots \end{aligned}$$

$E_{1,2,3}^{(i)}$  → determined through Passarino-Veltman reduction:  
proportional to inverse powers of the full Gram determinant (GD)

$$GD(p_1 + p_2 \rightarrow p_3 + p_4 + p_5) = \det(p_i \cdot p_j) \simeq f(E_3, E_4, \sin \theta_3, \sin \theta_4, \sin \phi_4)$$

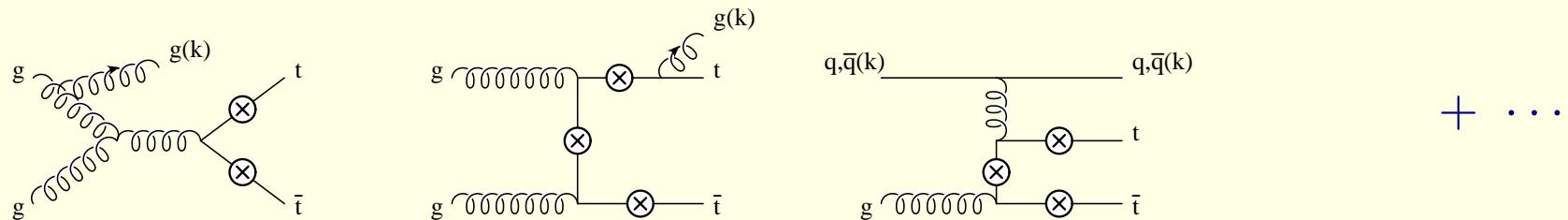
GD → 0 when two momenta become degenerate: spurious divergences.

We use two methods:

- Kinematic cuts to avoid numerical instabilities and extrapolation to the unsafe region using several algorithms.
- Eliminate all pentagon tensor integrals at the level of the amplitude square.

# $p\bar{p}, pp \rightarrow Q\bar{Q}H$ : $\mathcal{O}(\alpha_s)$ real corrections

Real gluon emission: IR singularities for  $2 \rightarrow 4$  process



Phase Space Slicing  $\longrightarrow$  isolate the region of the  $Q\bar{Q}h + g(q, \bar{q})$  phase space where  $s_{ik} \rightarrow 0$

$$s_{ik} = 2p_i \cdot k = 2E_i k^0 (1 - \beta_i \cos \theta_{ik})$$

$$\begin{aligned} &\longrightarrow \text{two cut-off method : } \left\{ \begin{array}{ll} \delta_s & (k^0 < \delta_s \sqrt{s}/2) \\ \delta_c & (1 - \cos \theta_{ik}) < \delta_c \end{array} \right. \\ &\longrightarrow \text{one cut-off method : } s_{min} \quad (s_{ik} < s_{min}) \end{aligned}$$

- 2CM : L.Bergmann, J.Owens, B.Harris (review), ...
- 1CM : W.Giele, N.Glover, D.A.Kosower, S.Keller, E.Laenen

In the Two Cutoff Method ( $\delta_s, \delta_c$ ):

$$\hat{\sigma}_{real}(ij \rightarrow Q\bar{Q}H + g) = \hat{\sigma}_{soft} + \hat{\sigma}_{hard/coll} + \hat{\sigma}_{hard/non-coll}$$

where

- $\hat{\sigma}_{soft} \longrightarrow E_g < \frac{\sqrt{s}}{2}\delta_s$
- $\hat{\sigma}_{hard/coll} \longrightarrow E_g > \frac{\sqrt{s}}{2}\delta_s$  and  $(1 - \cos \theta_{ig}) < \delta_c$

are computed analytically to extract IR singularities

$$\hat{\sigma}_{soft} \propto \int d(PS_3) \left( \int d(PS_g)_{soft} |\mathcal{A}_{soft}(ij \rightarrow Q\bar{Q}H + g)|^2 \right)$$

$$\hat{\sigma}_{hard/coll} \propto \int d(PS_3) \left( \int d(PS_g)_{coll} |\mathcal{A}_{coll}(ij \rightarrow Q\bar{Q}H + g)|^2 \right)$$

- $\hat{\sigma}_{hard/non-coll} \longrightarrow E_g > \frac{\sqrt{s}}{2}\delta_s$  and  $(1 - \cos \theta_{ig}) > \delta_c$

is computed numerically, since IR finite.

In the One Cutoff Method ( $s_{min}$ ):

$$\hat{\sigma}_{real}(ij \rightarrow Q\bar{Q}H + g) = \hat{\sigma}_{ir} + \hat{\sigma}_{hard}$$

where

- $\hat{\sigma}_{ir} \rightarrow s_{ig} < s_{min}$

is computed analytically to extract IR singularities

- cross all colored particles to final state
- work with color ordered amplitudes: easier matching between soft and collinear region
- crossing functions: to account for difference between i.s. and f.s. collinear singularities

- $\hat{\sigma}_{hard} \rightarrow s_{ig} > s_{min}$

is computed numerically, since IR finite.

Consider e.g.  $gg \rightarrow t\bar{t}H + g$ :

$$\hat{\sigma}_{real}^{H \rightarrow ggt\bar{t}+g} = \int d(PS_5) \overline{\sum} |\mathcal{A}_{real}^{H \rightarrow ggt\bar{t}+g}|^2 ,$$

where

$$\mathcal{A}_{real}^{H \rightarrow ggt\bar{t}+g} = \sum_{\substack{i,j,k=A,B,C \\ i \neq j \neq k}} \mathcal{A}_{ijk} T^i T^j T^k .$$

The amplitude square is made of three terms:

$$\begin{aligned} \overline{\sum} |\mathcal{A}_{real}^{H \rightarrow ggt\bar{t}+g}|^2 &= \frac{(N^2 - 1)}{2} \left[ \frac{N^2}{4} \sum_{\substack{i,j,k=A,B,C \\ i \neq j \neq k}} |\mathcal{A}_{ijk}|^2 \right. \\ &\quad \left. - \frac{1}{4} \sum_{\substack{i,j,k=A,B,C \\ i \neq j \neq k}} |\mathcal{A}_{ijk} + \mathcal{A}_{ikj} + \mathcal{A}_{kij}|^2 + \frac{1}{4} \left( 1 + \frac{1}{N^2} \right) \left| \sum_{\substack{i,j,k=A,B,C \\ i \neq j \neq k}} \mathcal{A}_{ijk} \right|^2 \right] \end{aligned}$$

with very definite soft/collinear factorization properties.

Soft singularities  $\longrightarrow$  straightforward

How to disentangle soft vs collinear region of PS with one cutoff?

Collinear limit for  $ig \rightarrow i'$ :  $s_{ig} \rightarrow 0$  ( $i = g_1, g_2$ )

$$\begin{cases} p_i = z p'_i \\ p_g = (1 - z) p'_i \end{cases}$$

Each  $\mathcal{A}_{ijk}$  (or linear combination of) proportional to  $(s_{ai} s_{ig} s_{gb})^{-1}$

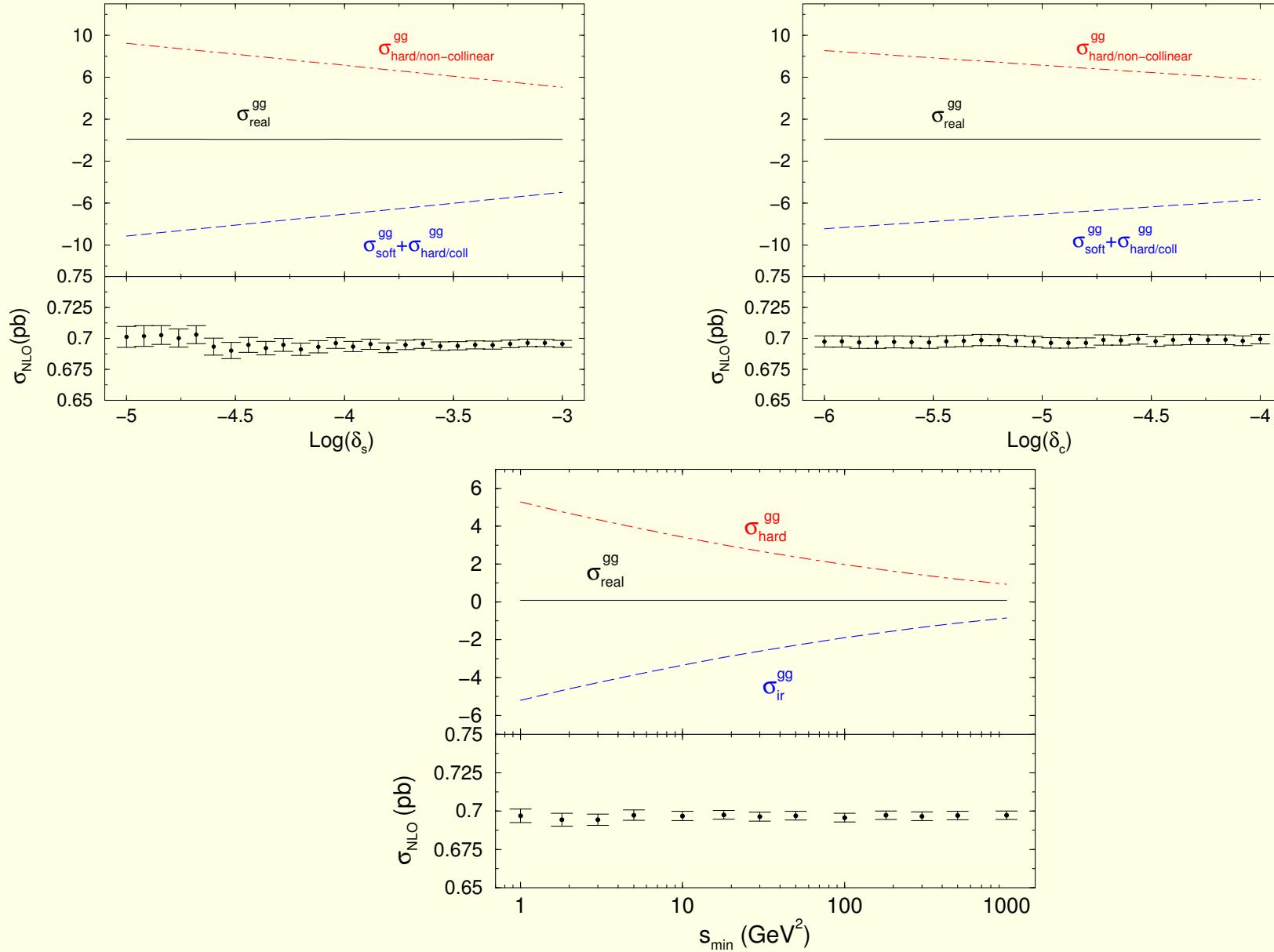
collinear region

$$\begin{cases} s_{ig} < s_{min} \\ s_{ai} > s_{min} \longrightarrow z s_{ai'} > s_{min} \longrightarrow z > z_1 = \frac{s_{min}}{s_{ai'}} \\ s_{gb} > s_{min} \longrightarrow (1 - z) s_{i'b} > s_{min} \longrightarrow z < 1 - z_2 = 1 - \frac{s_{min}}{s_{i'b}} \end{cases}$$

$z_1, 1 - z_2 \longrightarrow$  integration boundaries

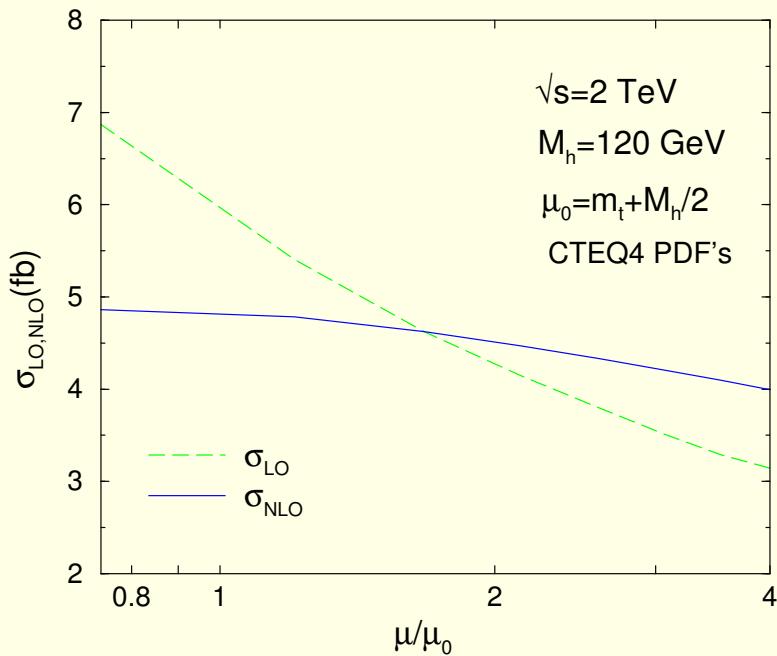
How to match with  $\hat{\sigma}_{hard}$ ? Match each term in  $|\mathcal{A}_{real}|^2$  separately.

# Cross section independent of the unphysical cutoff



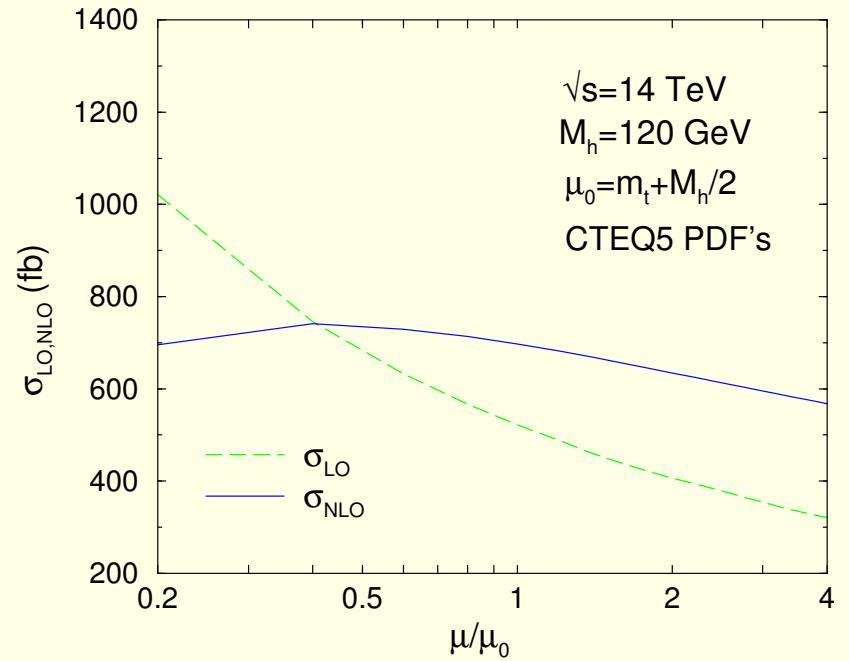
(LHC,  $M_H = 120$  GeV,  $\mu = m_t + M_H/2$ )

## LHC, $pp \rightarrow t\bar{t}H$ : NLO cross section



$$K = \frac{\sigma_{NLO}}{\sigma_{LO}} < 1$$

for most values of  $\mu$  and  $M_H$



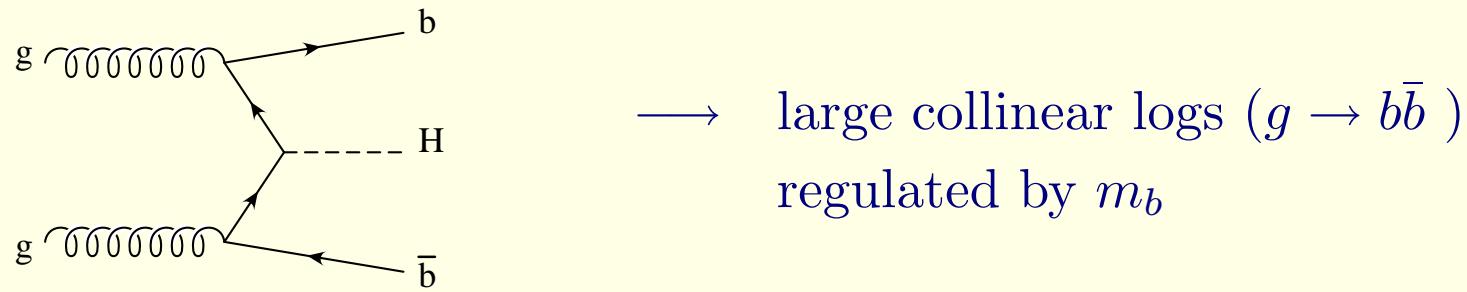
$$K = \frac{\sigma_{NLO}}{\sigma_{LO}} > 1$$

for most values of  $\mu$  and  $M_H$

Theoretical uncertainty reduced to about 15%

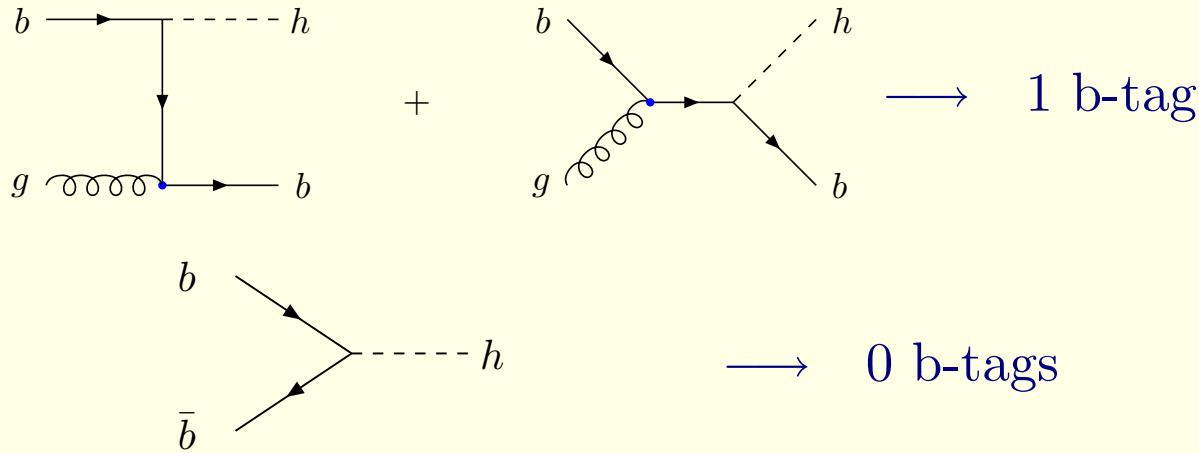
## $p\bar{p}, pp \rightarrow b\bar{b}H$ : exclusive vs inclusive cross section

- b-quarks identification requires tagging ( $p_T^b$  and  $\eta^b$  cuts):  
exclusive (1 b-tag, 2 b-tags) vs inclusive (0 b-tags) cross section.
- Large collinear  $\ln(\mu_H^2/m_b^2)$  arise in  $gg \rightarrow b\bar{b}h$  when final state b-quarks are collinear to initial state gluons



- Fully exclusive cross section (2 b-tags):
  - needs  $gg \rightarrow b\bar{b}h$ : two b's in final state
  - has no large logs:  $p_T^b$  cut select high  $p_T$  b's.
- NLO calculation drastically improves the stability of the cross section.

- More inclusive cross sections, two approaches:
  - Fixed (or four) flavor number scheme (FFS):  
fixed order approach, based on  $gg, q\bar{q} \rightarrow b\bar{b}H$  only.
  - Variable (or five) flavor number scheme (VFS):  
resum large logs in  $b$ -quark PDF.

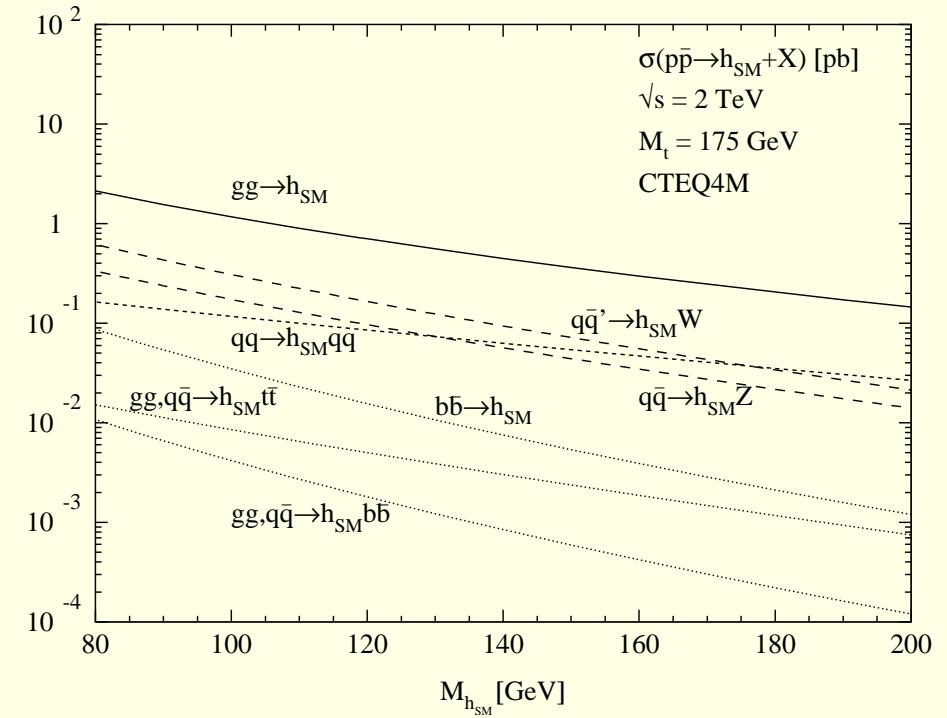
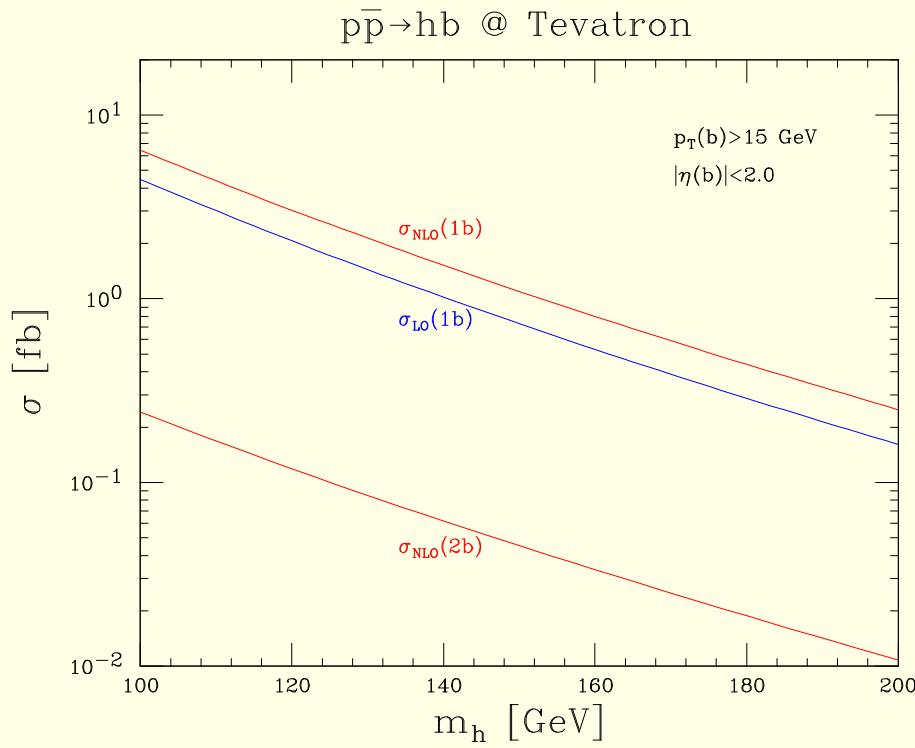


Perturbative series ordered in Leading and SubLeading powers of  $\alpha_s \ln(\mu_H^2/m_b^2)$ . Need to consider (avoiding double counting)

- ▷  $b\bar{b} \rightarrow H$  (known at NNLO)  $\longrightarrow \alpha_s^2 \ln^2(\mu_H^2/m_b^2)$
- ▷  $bg \rightarrow bH$  (known at NLO)  $\longrightarrow \alpha_s^2 \ln(\mu_H^2/m_b^2)$
- ▷  $gg \rightarrow b\bar{b}H$  (need LO, known at NLO)  $\longrightarrow \alpha_s^2$

## Inclusive versus Exclusive modes

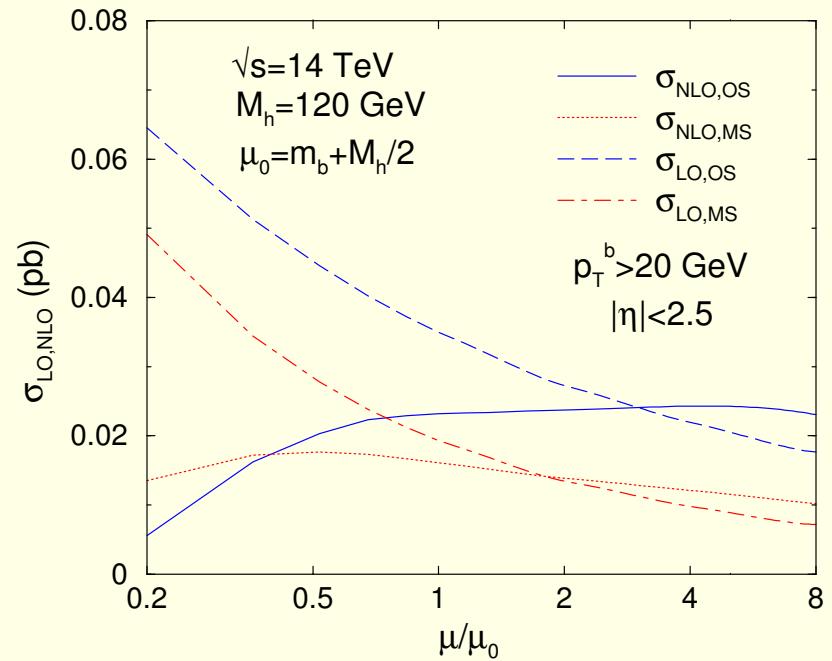
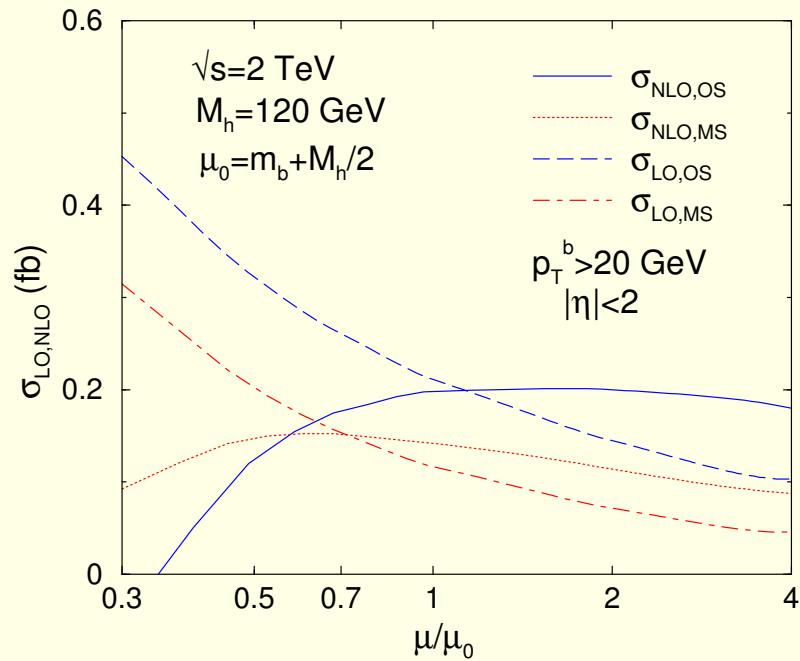
- More inclusive cross sections are larger.



- More exclusive modes have much smaller background.
- Only exclusive modes probe the  $b\bar{b}H$  coupling unambiguously.

## Exclusive cross section for $p\bar{p}, pp \rightarrow b\bar{b}H$ : 2 b-tags

Use high  $p_T$   $b$ -quarks to suppress background: need NLO ( $q\bar{q}$ ) $gg \rightarrow b\bar{b}H$

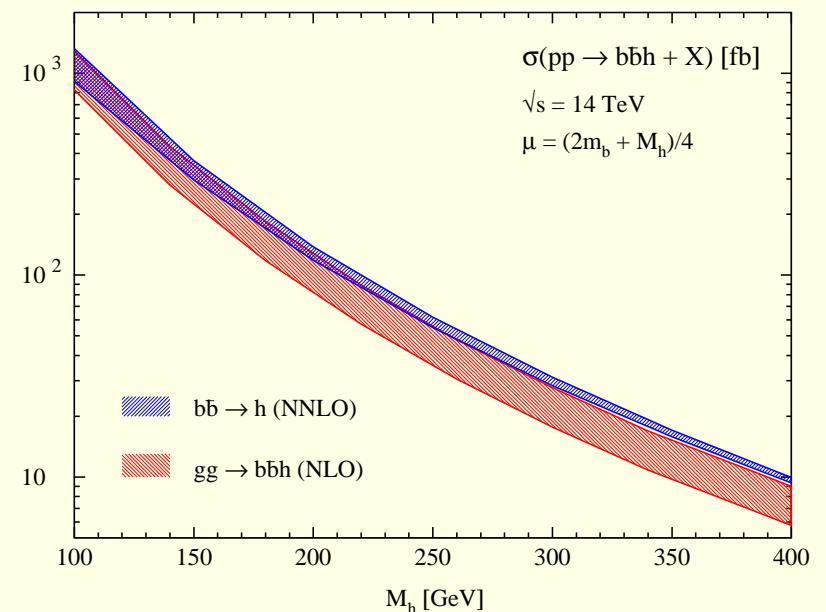
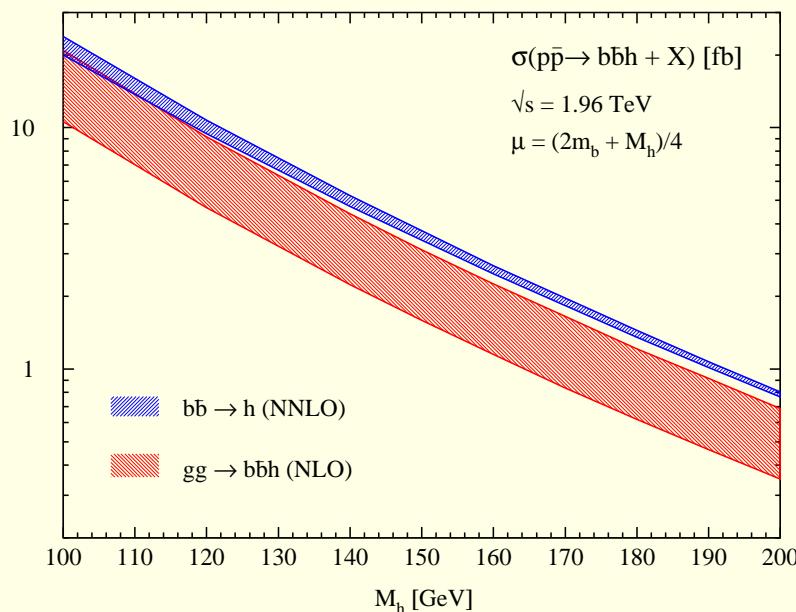
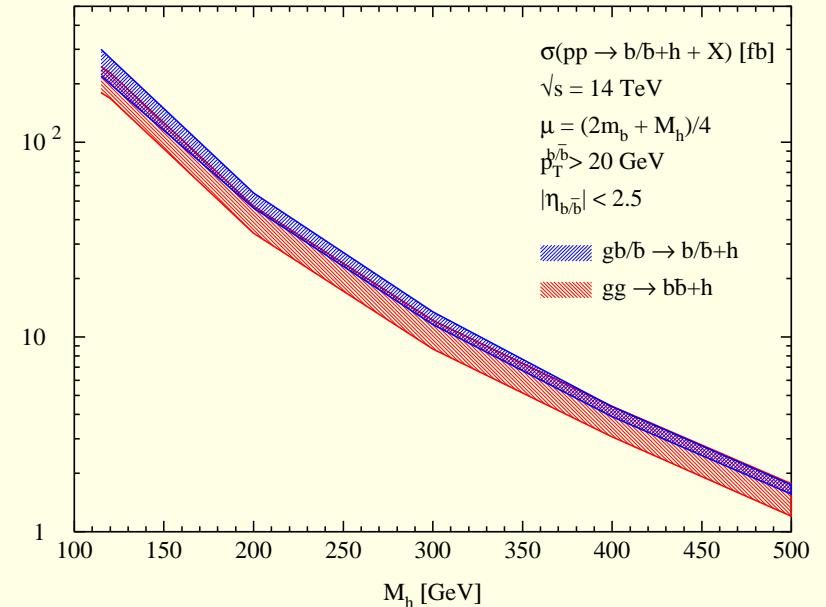
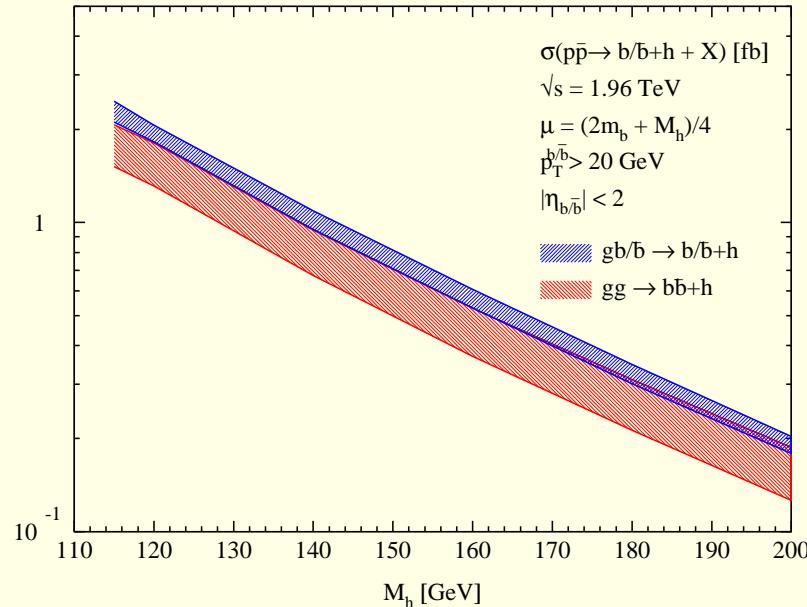


Non trivial dependence on renormalization of  $m_b(\mu)$  in bottom quark Yukawa coupling:  $OS, MS \rightarrow$  renormalization scheme of  $y_b = m_b/v$ .

Theoretical uncertainty: 15% (scale dep.), 15% (ren. scheme dep.)

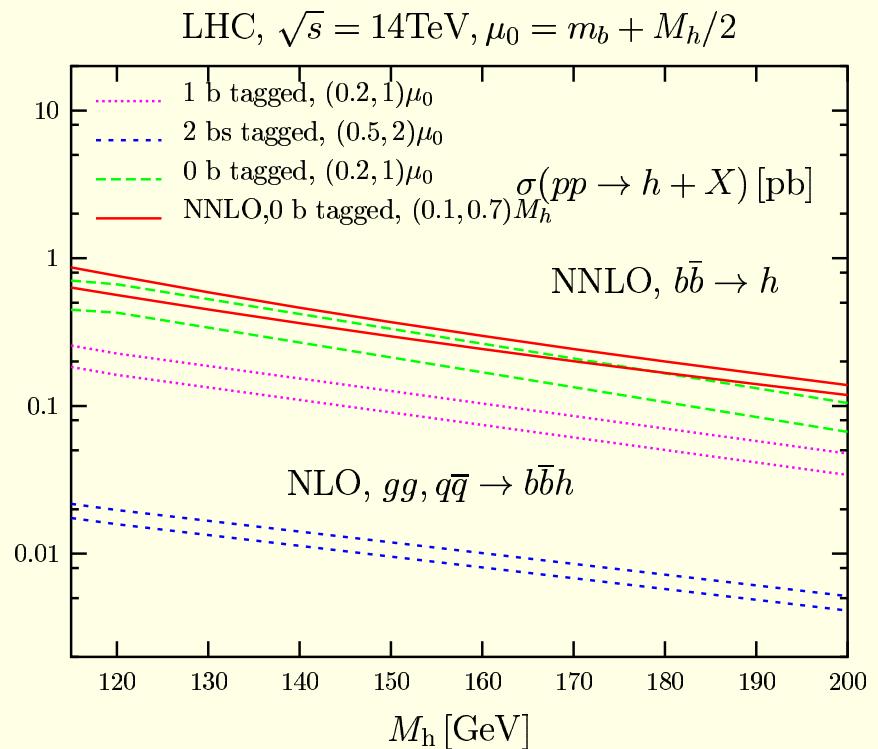
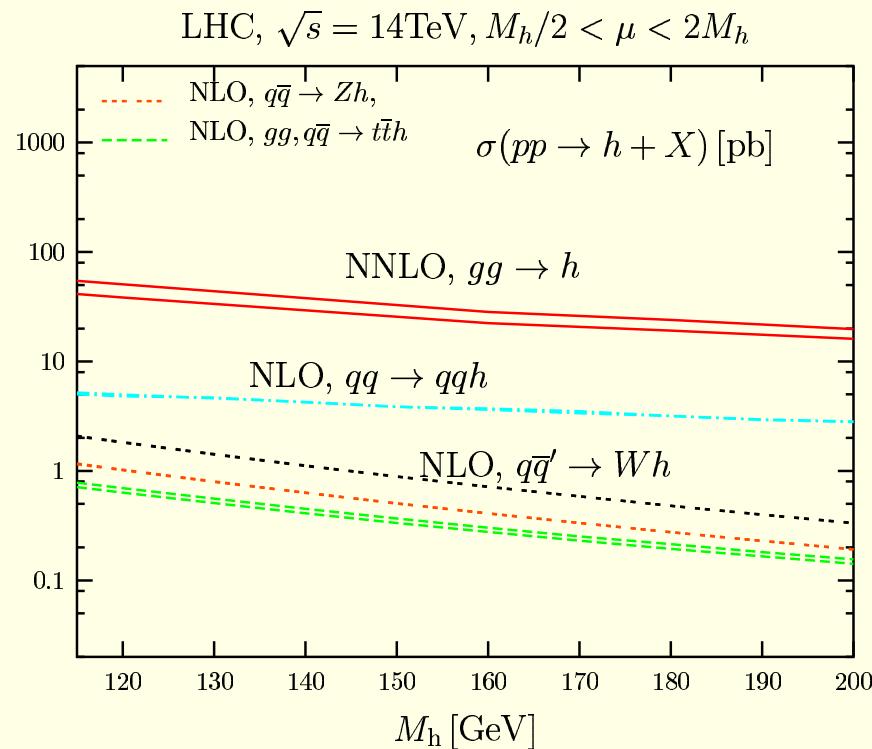
# 1b-tag and 0b-tag modes: comparison between FFS and VFS

(Les Houches Workshop, 2003-2004)



# Overview

QCD predictions for total cross sections to Higgs production processes are under good theoretical control:



Caution:

- ▷ uncertainties only include  $\mu_R/\mu_F$  dependence
- ▷ uncertainties from PDF's are not included (but should improve)