

Ideal Gas Law

- Pressure, volume, and temperature of a gas are related to how much of the gas (N , # of molecules):

$$pV = NkT$$

Boltzmann constant,
 $k = 1.38 \times 10^{-23} \text{ J/K}$

- Alternate form (Chemistry): $pV = nRT$

- Reminder: T absolute, in Kelvins # of moles

Using Ideal Gas Law

- Usually # of molecules constant, so Nk is constant

$$\rightarrow \frac{pV}{T} = \text{const}$$

- E.g., new temp if pressure, volume change:

$$T_{\text{new}} = \frac{p_{\text{new}} V_{\text{new}}}{p_{\text{old}} V_{\text{old}}}$$

- Changing between # of molecules and mass:

- Atomic mass unit (~avg. mass of proton/neutron):

$$1 \text{ u} = 1.66 \times 10^{-27} \text{ kg}$$

- Look up how many amu for a particular atom

- Add all the atoms in a molecule: get mass of molecule

Energy/speed of Gases

- Temperature is really just a measure of “internal” (non-macroscopic) energy
- Gases: temperature directly related to (translational) kinetic energy

$$K_{tot} = \frac{3}{2} N k T$$

- Average kinetic energy per molecule:

$$\bar{K} = \frac{3}{2} k T = \frac{1}{2} m \bar{v}^2$$

- Root of average square speed (**thermal speed**):

$$v_{th} = \sqrt{\bar{v}^2} = \sqrt{\frac{3 k T}{m}}$$