

The determined value is subject to the following systematic error: the small ball is also attracted by the more distant second large ball, albeit with a much lower force (refer to Fig. 5).

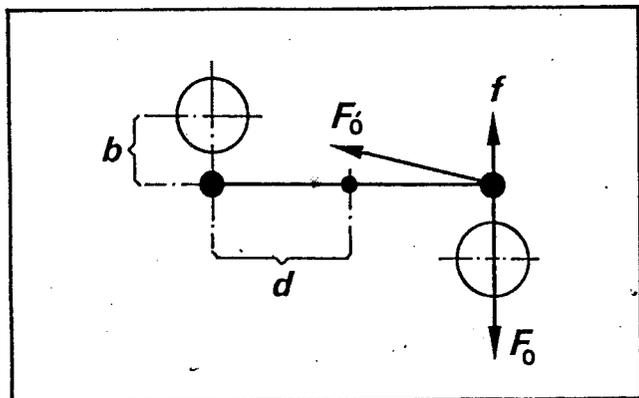


Fig. 5: Calculating the correction factor

In accordance with the gravitation law, this force is given by

$$F_0 = 2G \frac{m_1 m_2}{b^2 + 4d^2}$$

and has a component f opposed to the force F_0 to be measured

$$f = 2G \frac{m_1 m_2}{b^2 + 4d^2} \frac{b}{\sqrt{b^2 + 4d^2}} = \beta F_0,$$

if β is the fraction by which the observed force F_0 is reduced.

$$\beta = \frac{b^3}{(b^2 + 4d^2) \sqrt{b^2 + 4d^2}}$$

$\beta = 0.075$ where $d = 0.05$ and $b = 0.0465$ m. The value for G obtained without this correction must therefore be increased by 7.5 %.

For our measurement example, we thus obtain

$$\underline{G = 6,698 \cdot 10^{-11} \text{m}^3 \text{kg}^{-1} \text{s}^{-2}}$$

instead of the theoretical value

$$G = 6,705 \cdot 10^{-11} \text{m}^3 \text{kg}^{-1} \text{s}^{-2}.$$